

# FIRST-PRINCIPLES STUDY OF INTERSTITIAL HYDROGEN IN YTTRIA-STABILIZED ZIRCONIA (YSZ)

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# INTRODUCTION



Hydrogen is a common impurity in materials (semiconductors, oxides, microelectronics devices) sometimes intentionally introduced.

Passivation of defect and trapping centers (e.g. Si DB's at Si/SiO<sub>2</sub> interface)



Experimentally it is difficult to obtain a clear signature of isolated hydrogen (mobile/low migration barrier, forms defect associates, e.g. complexing with dopants in Si.)



Reliability issues in microelectronics, degradation of electrical properties of MOSFETs (under irradiation and electrical stress): increase of interface traps



A lot about what we know for hydrogen in solids comes from calculations based on density-functional theory (DFT), e.g. defect reactions with participating H

Electronic behavior of H: source of n-type conductivity

amphoteric impurity

Charge-transition levels  $E(+/0)$  (donor level) and  $E(+/-)$  wrt CBM

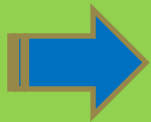
(Van de Walle and Neugebauer 2003, Kiliç and Zunger 2002, J. Robertson's group)

# Muonium spectroscopy

$\text{Mu}^+ - \text{e}^-$  : pseudoisotope of hydrogen ( $m_\mu \sim \frac{1}{9} m_p$ )

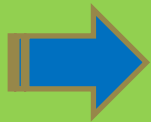
Lifetime: 2.2  $\mu\text{sec}$

Cubic polycrystalline YSZ (9.5 mol%  $\text{Y}_2\text{O}_3$ ) (Cox et al., JPCM 2006)

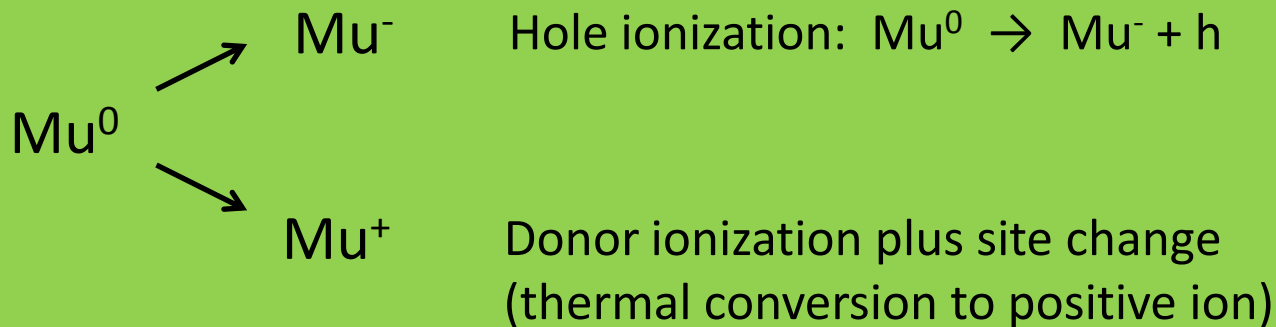


Low T : atomic muonium co-exists with shallow-donor states

(Atomic : high isotropic hyperfine constant, within 20% of free-atom value)



At and above RT: conversion of paramagnetic to diamagnetic fraction(s)



Density-functional theory GGA-PBE functional for exchange-correlation

VASP code (Vienna Ab-initio Simulation Package) (Kresse, Hafner and Furthmüller, 1993-96)

Projector-augmented-wave method (PAW) /  $E_{\text{pw}} = 470 \text{ eV}$  4k points in the IBZ

Semi-core 4s and 4p states as valence for both Zr and Y

Hybrid-functional approach (Heyd, Scuseria, Ernzerhof 2006)

Admix an amount of exact non-local HF exchange to the PBE exchange

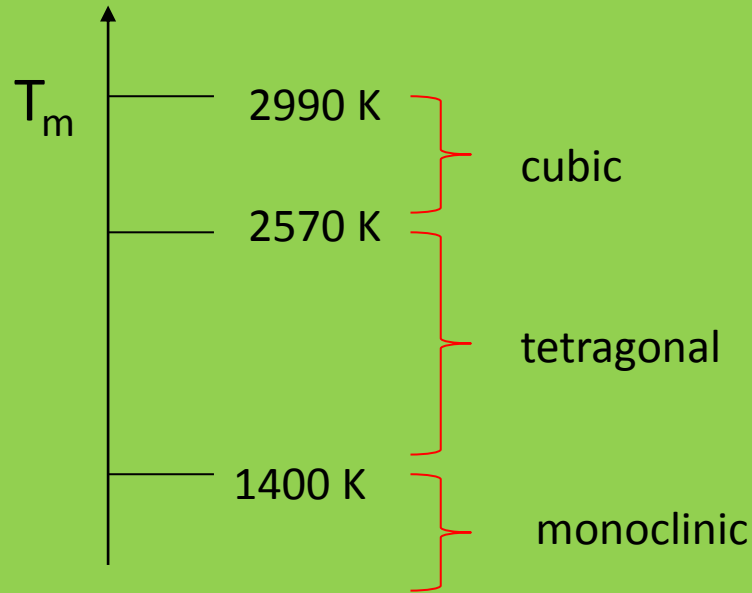
$$E_{\text{xc}}^{\text{HSE06}} = \frac{1}{4} E_{\text{x}}^{\text{HF,SR},\mu} + \frac{3}{4} E_{\text{x}}^{\text{PBE,SR},\mu} + E_{\text{x}}^{\text{PBE,LR},\mu} + E_{\text{c}}^{\text{PBE}}$$

( $\mu$  : spatial decay of HF exchange)

## GOALS

- ➡ Different minimum-energy configurations of hydrogen in the lattice for a given charge state ( $\text{H}^0$ ,  $\text{H}^+$ ,  $\text{H}^-$ ) .
- ➡ Formation energies and charge-transition levels,  $E(q/q')$ , in the gap.
- ➡ Stability analysis of neutral  $\text{H}^0$  in the lattice : site changes of  $\text{H}^0$ , migration paths, find MEPs, TSTs and corresponding barriers through Nudged-Elastic-Band (NEB) method (DFT-PBE).

Zirconia is an important ceramic commonly used as electrolyte in solid oxide fuel cell (SOFC) technology. High electrical conductivity via oxygen vacancies.



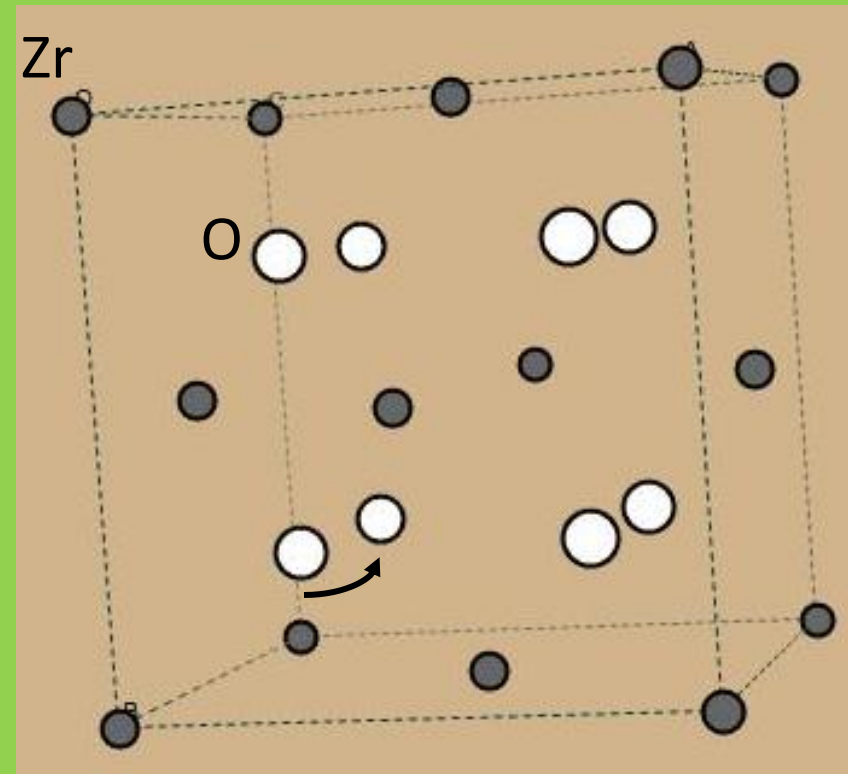
Cubic phase stabilized at lower T by doping with M<sub>2</sub>O<sub>3</sub> or MO oxides

Oxygen vacancies compensate the charge of the substitutional defects

IDEAL UN-DOPED  
CUBIC FLUORITE ZrO<sub>2</sub>

Zr → FCC

O → T<sub>h</sub>



Cubic YSZ :  $\geq 8 \text{ mol } \% \text{ Y}_2\text{O}_3$

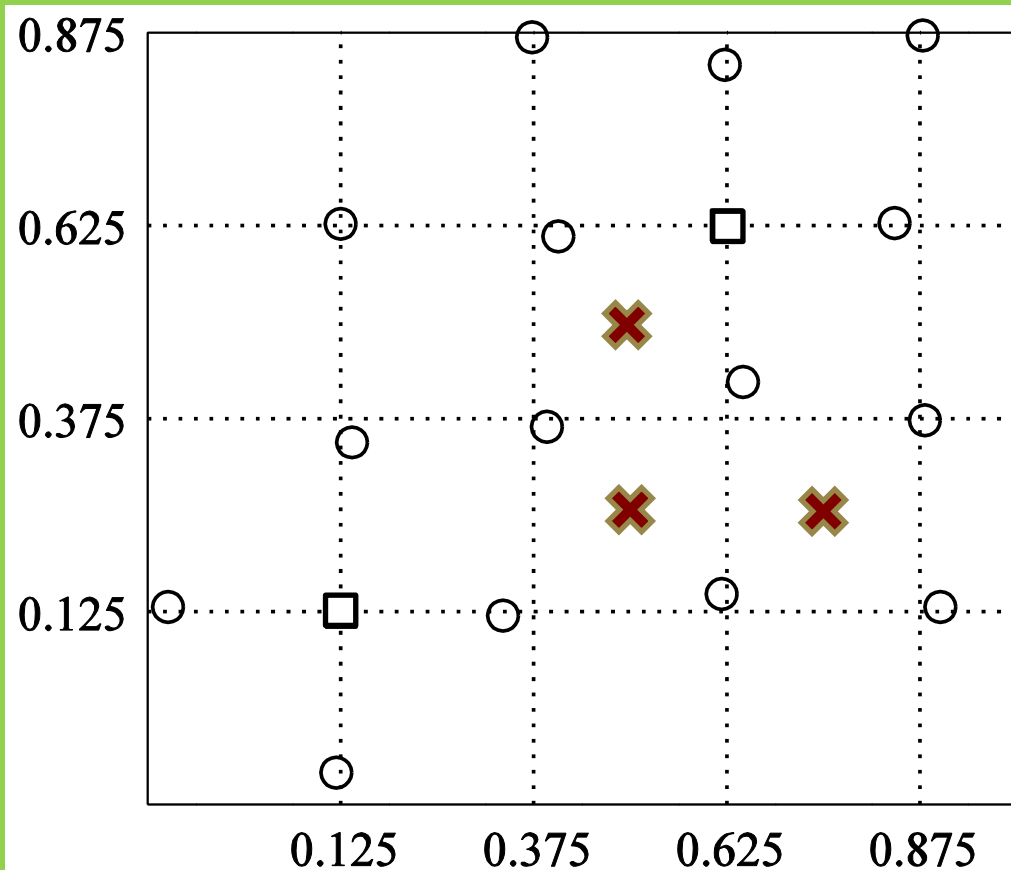
# Cubic YSZ cell ( $2 a_{\text{latt}} \times 2 a_{\text{latt}}$ )

10.3 mol%  $\text{Y}_2\text{O}_3$

Corners: ideal O sites in fluorite lattice

Oxygen sublattice

□ Oxygen vacancies  
(at least 5<sup>th</sup> nn)



$\text{O}_{\text{NN}}$ 's predominantly displace  
along [001] directions

$V_{\text{O}} - \text{O}_{\text{NN}}$  attraction

$\Delta s(\text{O}_{\text{NN}}) : 0.22 - 0.56 \text{ \AA}$

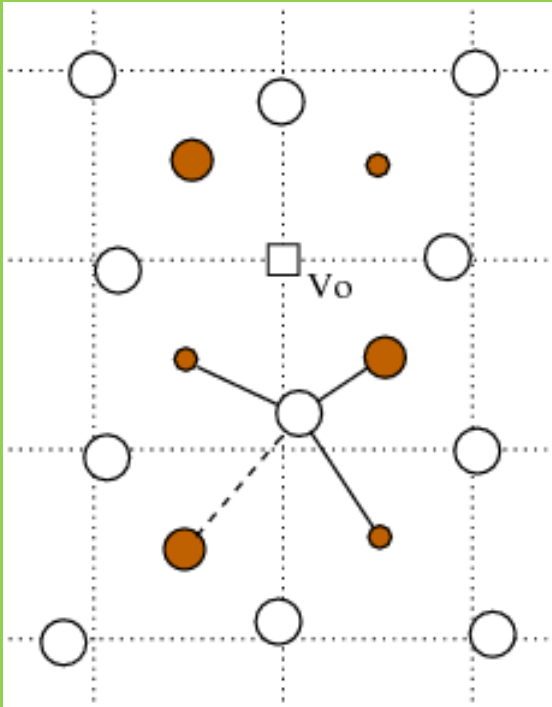
$\Delta s(\text{O}_{\text{NNN}}) : 0.12 - 0.30 \text{ \AA}$

$\Delta s(\text{Zr}_{\text{NN}}) : 0.13 - 0.25 \text{ \AA}$

$\Delta s(\text{Zr}_{\text{NNN}}) : 0.02 - 0.17 \text{ \AA}$

## Bulk crystal YSZ (10.3 mol%)

□ : Oxygen vacancies ( $V_o$ )



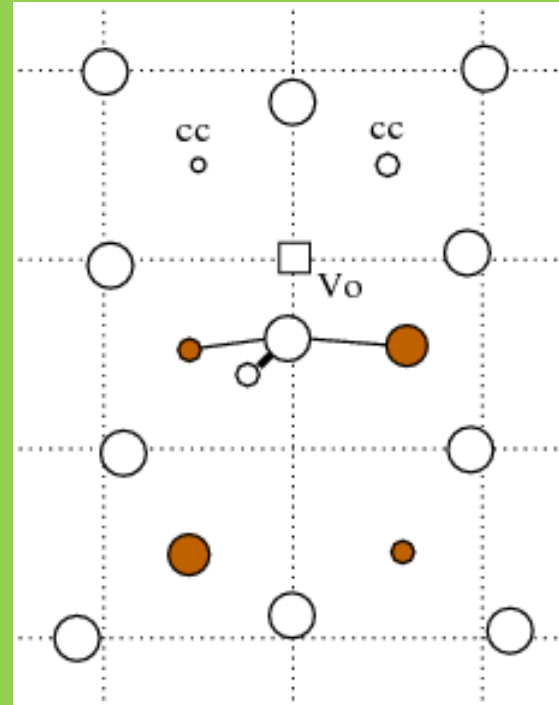
 Zr

## Largest distortions near oxygen vacancies

O ions attracted to NN vacancies

CN<sub>0</sub> becomes 3 near Vo's

## Minimum-energy hydrogen configurations

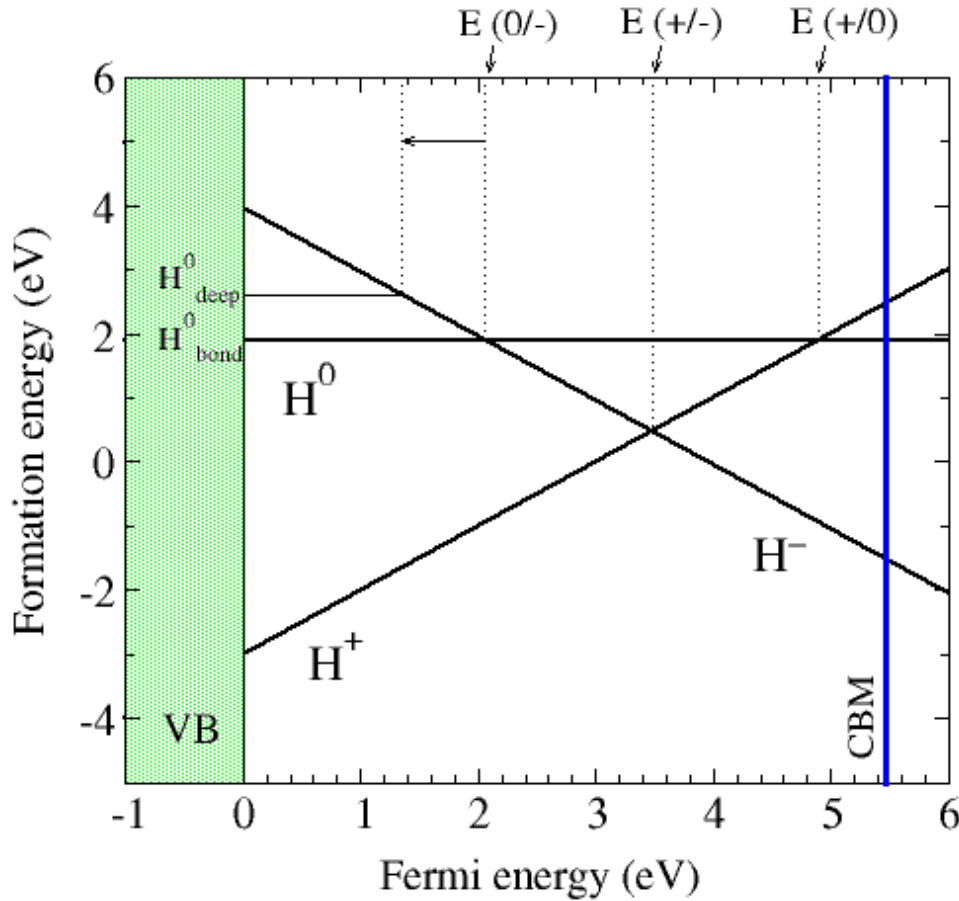
 $\text{O} \quad \text{H}$ 

OH- bond-type configurations } All H charge states  
O-H: 0.98Å (large lattice relaxation)

$$\text{CN}_\text{O} : 2 + 1 \quad (\text{Zr-O} : 2.10 - 2.30 \text{ \AA})$$

H at deep interstitial sites  
(minimal relaxation) : cc, Vo }  $H^0$  and  $H^-$

# Formation energies and charge-transition levels $E(q/q')$



## Amphoteric behavior for H

Transition level  $E(+/-)$  deep in the gap:  $E_{\text{VBM}} + 3.50 \text{ eV}$

Hydrogen not source of n-type conductivity

## Deep acceptor and donor levels

Not consistent with shallow-donor behavior observed by  $\mu\text{SR}$  (inferred muonium ionization energies  $E_D \sim 10 - 30 \text{ meV}$ )

$$E_{\text{form}}^{(q)} = E_{\text{tot}}^{(q)} - E_{\text{tot}}^{\text{bulk}} - \mu_{\text{H}} + q(E_{\text{F}} + E_{\text{VBM}})$$

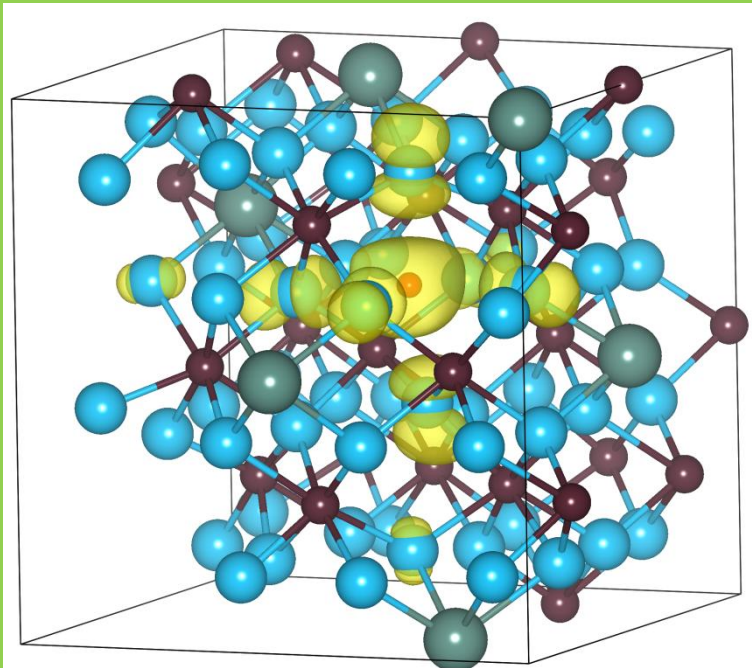
Delocalized solution unstable



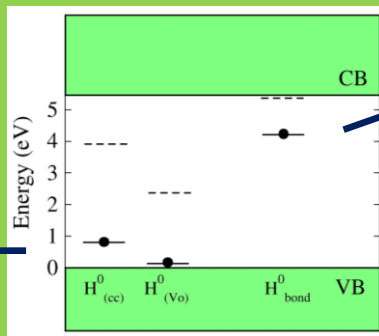
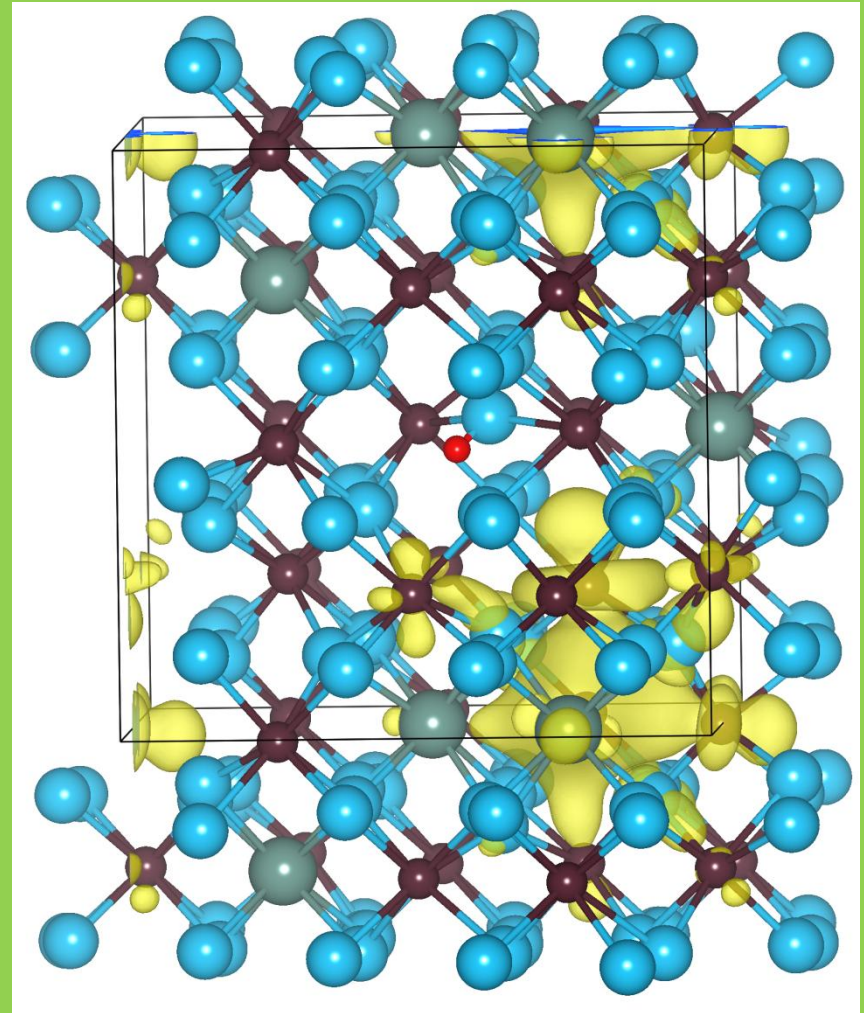
# Nature of defect levels of neutral $H^0$ configurations

Deep interstitial  $H^0$  configurations

Higher energy



Bond-type configurations



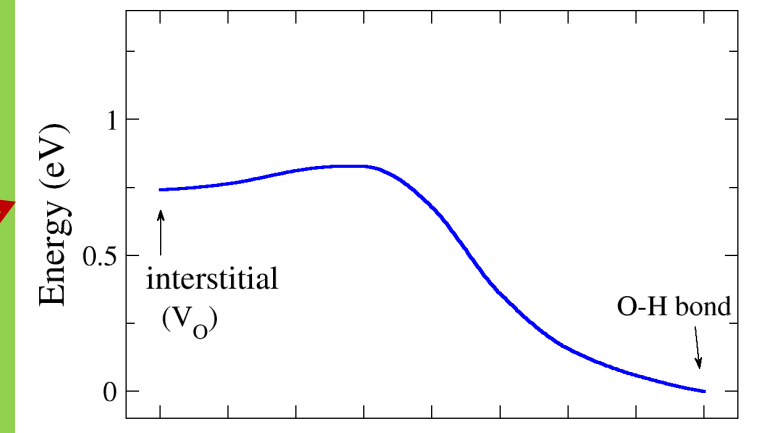
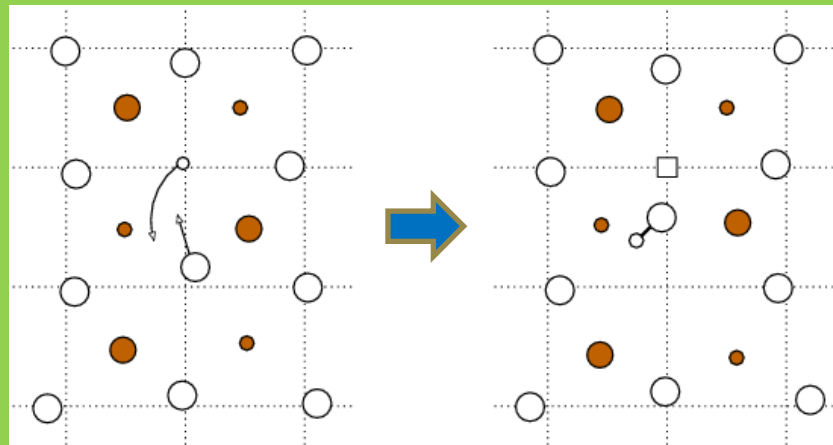
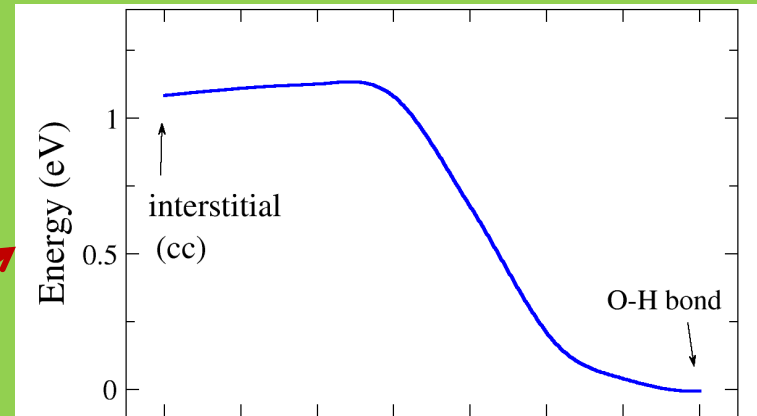
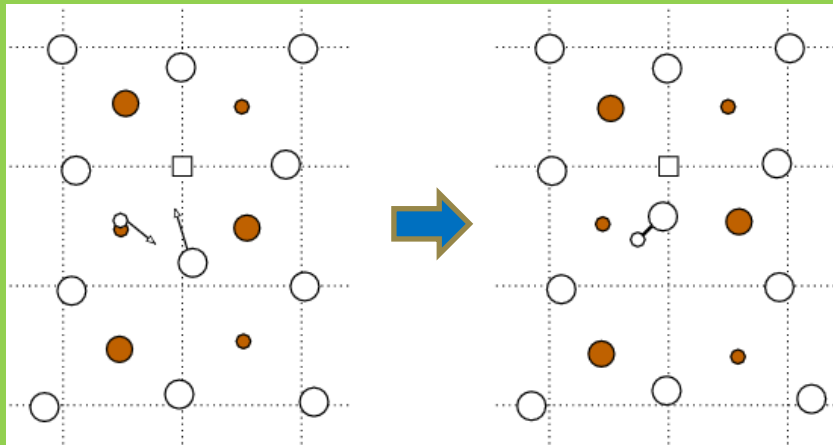
$E_{CBM}$   
- 1.2 eV

Excess  $e^-$  on neighboring Zr ions and empty cube centers of O sublattice

# Neutral $H^0$ : interstitial – to – bond site changes

Local transformation between two nearby configurations: requires simultaneous displacements of  $H^0$  and O's of the host

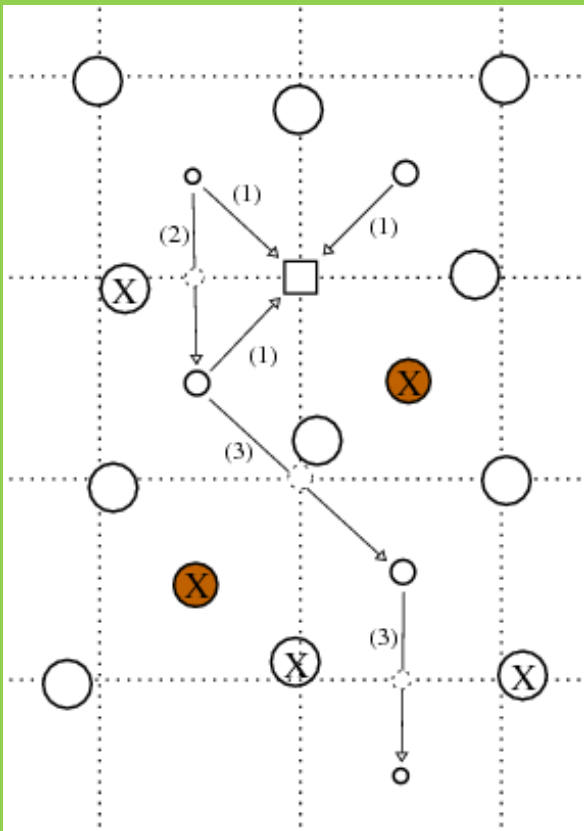
Energy for minimum-energy paths (MEPs) (NEB method)



REACTION COORDINATE

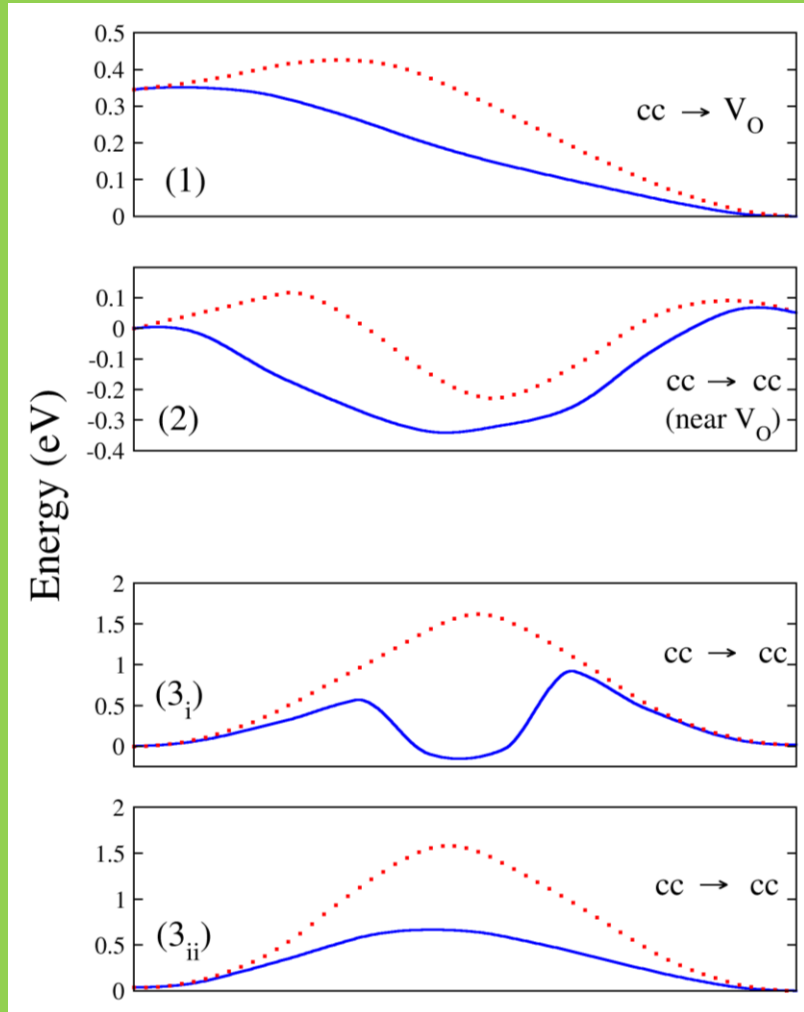
# Explore the global character of the migration behavior of $H^0$

Migration paths connecting interstitial sites in the lattice



## MEPs and barriers

..... rigid-lattice condition  
—— full relaxation



at / near  $V_O$ 's

Away from  $V_O$ 's

# SUMMARY



H incorporates in cYSZ (10.3 mol%) in two distinct configurations

Interstitial configurations  $H_{\text{int}}$  (cc and Vo sites) (acceptor sites)

Bond-type configurations  $H_{\text{bond}}$  (donor sites)



Amphoteric behavior of hydrogen :  $E(+/-)$  level deep in the gap

Donor level of  $H^0$ : deep in the gap centered on neighboring Zr atoms



NEB calculations of MEPs and barriers for neutral H:

Transformation of interstitial to bond configuration:  $H_{\text{int}} \rightarrow H_{\text{bond}}$

Small barrier but requires rearrangement of host lattice (attain equilibrium)



Vo's play important role in migration behavior of neutral H

Reduce barriers in their vicinity : facilitate instability towards  $H_{\text{bond}}$

Away from Vo's : higher  $E_{\text{act}}$  are needed for  $H_{\text{int}}$  to migrate