

# The muon site: a toolbox

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**Aim:** put together an easily shearable tool to identify the muon site.

## Functions and strategies:

1. Open software with simple mathematics and graphics (matlab like)
2. Access to a crystallographic library, to define and visualize lattice & magnetic structure
3. **Exploration of tentative muon sites:**
  - Simple dipolar sums, with given point-like magnetic moments
  - Point charge electrostatic potential, e.g. constrained on spheres around anions
4. **DFT calculation of muon site**
  - Full muon potential
  - Zero point motion
  - Full hyperfine field (contact and dipolar)
5. Documentation, both embedded and web based

## 1. Python <http://www.python.org/>



Open software, available on all OS

Quick interface to software in any other language, see bona below

ipython, specialized for interactive use, with more extensive help

<http://ipython.scipy.org>

Matlab-like dialect <http://matplotlib.sourceforge.net/>

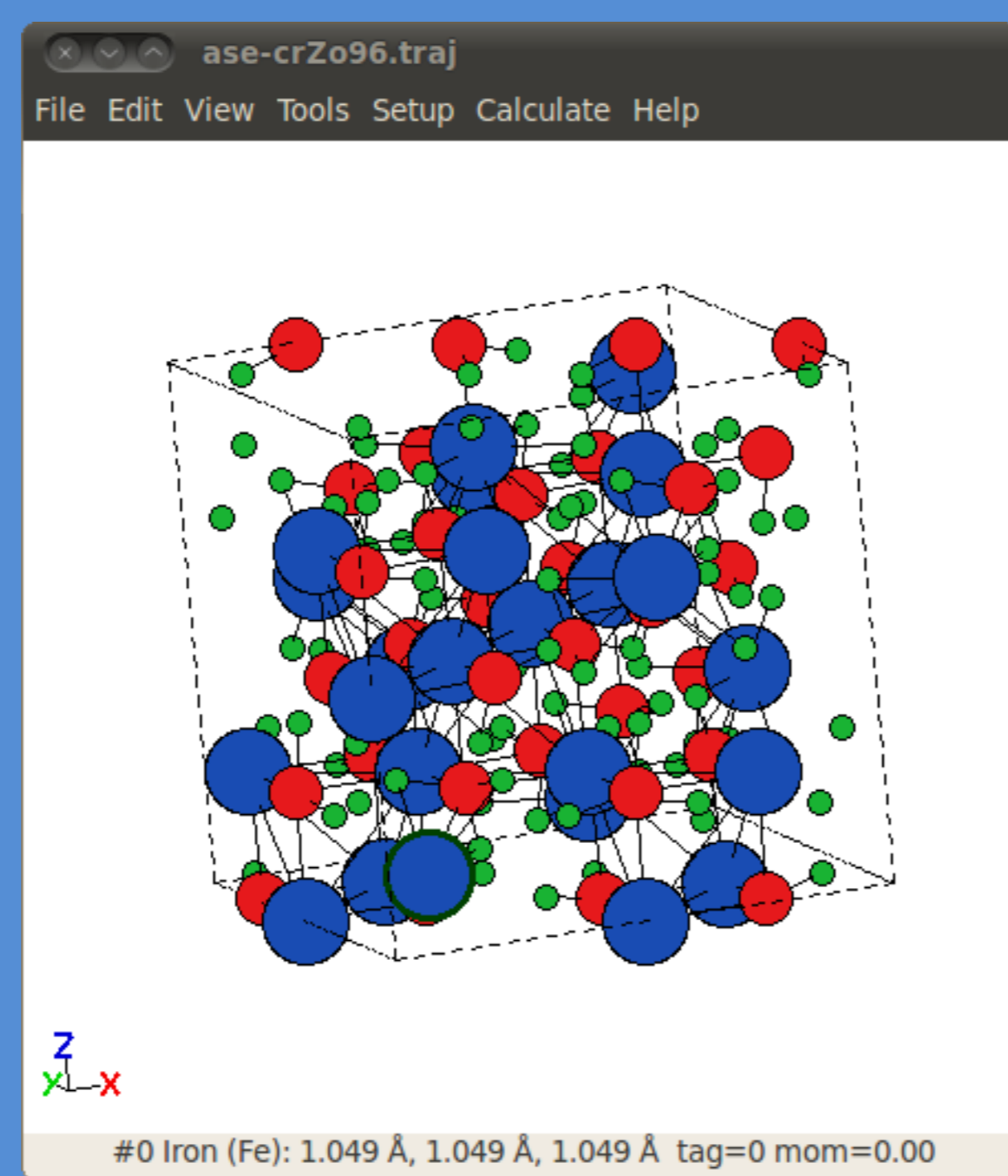


## 2. ASE: Atomistic Simulation Environment

<https://wiki.fysik.dtu.dk/ase>

### Includes

full crystal symmetry groups  
lattice visualization  
initial magnetic moments and ion charges  
interface to many DFT calculators



```
import ase
import numpy as np
from ase.lattice.spacegroup import crystal
a = 8.3940
fe3o4=crystal(['Fe','Fe','O','H'],
              basis=[(0.12500, 0.12500, 0.12500),
                    (0.5, 0.5, 0.5),
                    (0.25480, 0.25480, 0.25480),
                    (0.285, 0.285, 0.1302)],
              setting=2,
              spacegroup=227, cellpar=[a, a, a, 90, 90,
              90],
              size=(1,1,1), pbc=False)
ase.visualize.view(fe3o4)
```

## 3. ASE

Zero-order muon site validation. Reproduce two types of published results

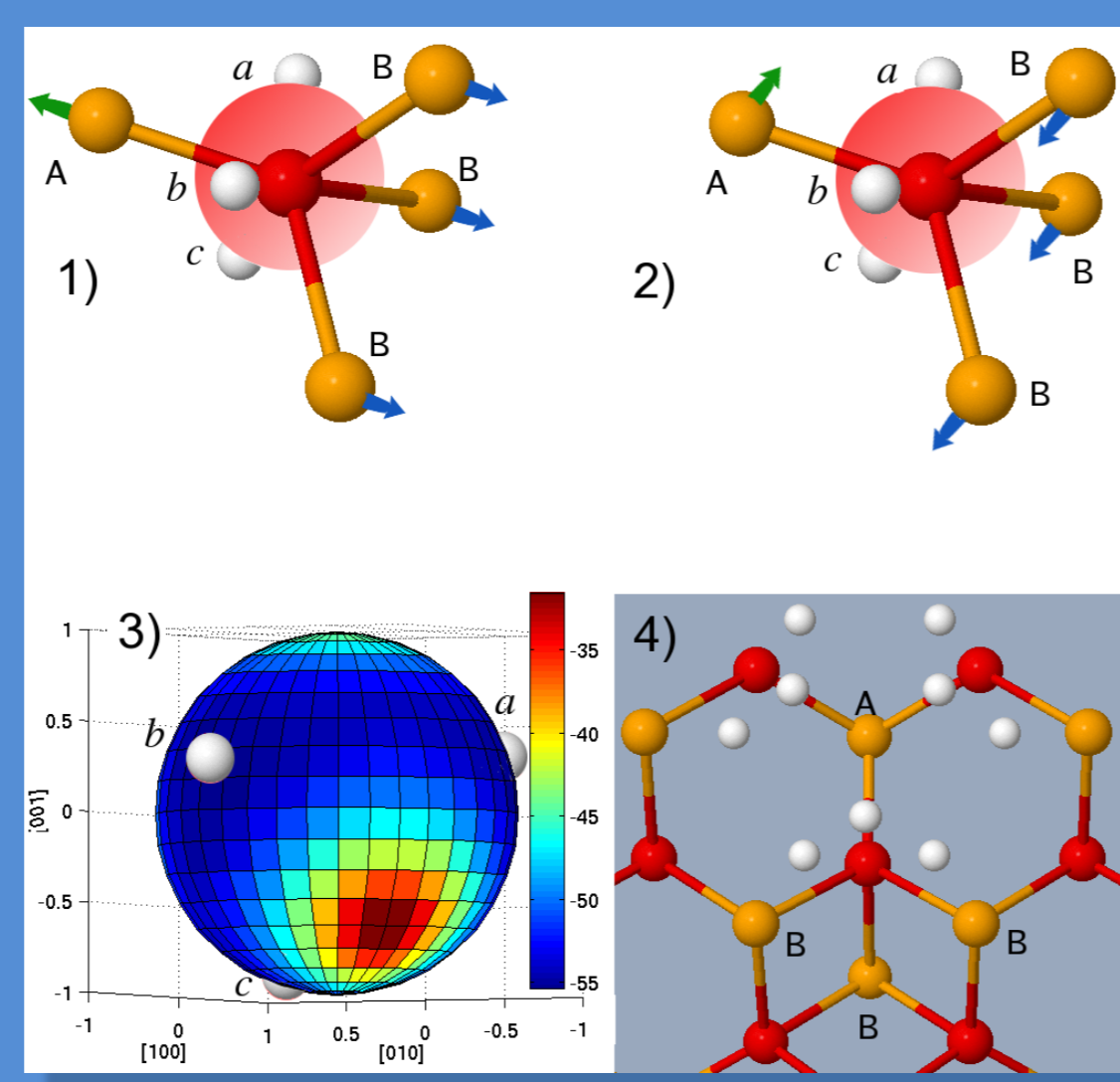
- Those obtained by simplified strategies, such as  $\text{YBa}_2\text{Cu}_3\text{O}_6$  [1] and  $\text{Fe}_3\text{O}_4$  [2]:
  - find point charge potential  $V$  minima,
  - check dipolar sums against local field  $B_\mu$

Dipolar sum code  
5 declarations  
12 lines of code with check of convergence

Point charge potential with Ewald's trick  
4 declarations  
26 lines of code

See also  
<http://www.fis.unipr.it/~derenzi/dispense>

(node pmwiki.php?n=MuSR.ASEStart#potential)



- Those obtained by DFT (see box 4. on the right)

## 5. Documentation

Embedded, ipython provides

- tabbed completion of commands
- interactive help on each available command just by entering command?

Web based, a wiki (under construction) with instructions on

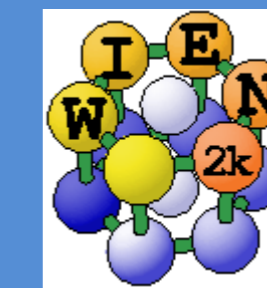
- how to install the various bits
  - Python itself
  - ASE
  - The chosen DFT
  - The toolbox
- examples of how to run the toolbox

## 4. Density Functional Theory calculator

Many different programs can be installed and invoked with a simple python command:



More can be interfaced, including Wien2k



One is already included and allows simple calculations



Finding the muon site by DFT may be anything between *straightforward* (ionic crystal) and a *subtle art* (the muon bond in a lattice with *all-electron* atoms, typically rare earths)

## 4. Density Functional Theory by F. Bernardini

Example, cfr. [3]:  $\text{LaFeAsO}$

$$V = V_\mu = -V_e \quad \text{only Coulomb!}$$

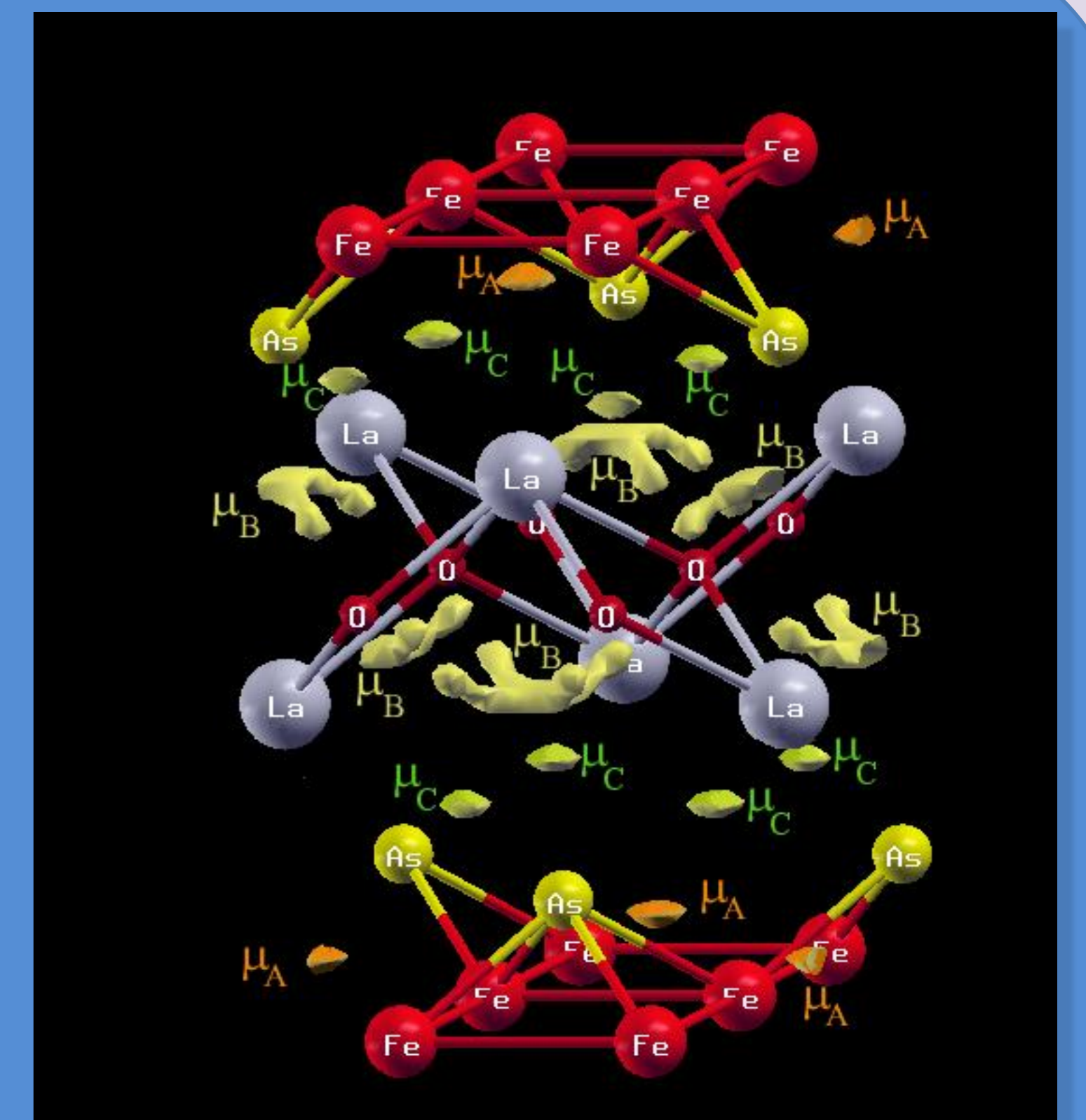
Muon site(s) volume

- centered at  $\min(V)$
- defined by harmonic zero energy  $E_0$  within the isopotential surface

$$V = \min(V) + E_0$$

	$\mu_A$	$\mu_B$	$\mu_C$
$V(\text{eV})$	$0^*$	0.55	0.94
$E_0(\text{eV})$	0.15	0.12	0.16

\* arbitrary



## To be done

- Documentation
- Packaging, distribution, installation instructions
- Choice of suitable DFT for ASE
- Full hyperfine field calculation
- Muon bond
- More extensive validation

## Acknowledgements

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## References

- [1] M. Weber, P. Birrer, F. N. Gygi, B. Hitti, E. Lippelt, H. Maletta, A. Schenck, Hyperfine Interactions **63**, 207 (1990)
- [2] M. Bimbi, G. Allodi, R. De Renzi, C. Mazzoli, H. Berger, Phys. Rev. B **77**, 045045115 (2008)
- [3] H. Maeter *et al.*, Phys. Rev. B **80**, 094524 (2009)