



# Muon Target Simulations

Adriana Bungau  
(Bob Cywinski)

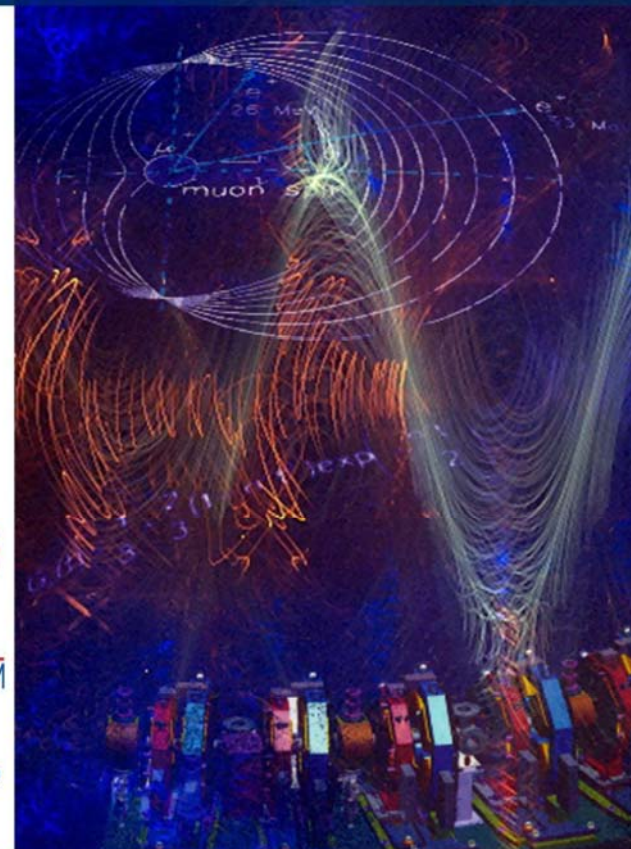


# Motivation



....an FP6 NMI3 funded workshop at the Cockcroft Institute, Daresbury, in April 2008

## Towards a Next Generation European Muon Source



nmi3

BASROC  
CONFORM



NMI3/CONFORM Workshop, Cockcroft Institute, Daresbury 8/9 April 2008

NMI3, Zurich , 30 March '09



# Motivation

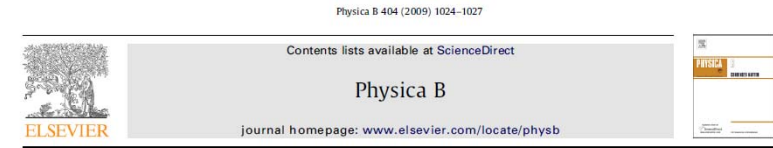


# Motivation

A stand-alone optimised muon facility could deliver x100 intensity gains in pulsed mode and comparable intensity to PSI in CW mode

A 1Gev, 0.5mA Fixed Field Alternating Gradient proton accelerator at KHz frequencies would be an appropriate and cost effective driver

	Cyclotron	FFAG	Synchrotron
<b>Energy ~ 1 GeV</b>	No	Yes	Yes
<b>Current &gt; 1 mA</b>	Yes	Yes	No
<b>Frequency</b>	CW	0.1 – 2 kHz	30 – 60 Hz
<b>Pulse length</b>	Continuous (~ 1 ns)	10 ns – 1 $\mu$ s	100ns to ~ 1 $\mu$ s
<b>Beam size ~mm<sup>2</sup></b>	No	Yes	No
<b>Extraction efficiency</b>	Good	Good	Good
<b>Operation</b>	Easy	Easy	Not easy
<b>Maintenance</b>	Hard	Normal	Normal
<b>Static fields</b>	Yes	Yes	No
<b>Size</b>	Moderate	Compact	Very large
<b>Mult. beam extraction</b>	No	Yes	Difficult
<b>Construction cost</b>	High	Moderate	Very high
<b>Existing technology</b>	Yes	No!	Yes



## Towards a dedicated high-intensity muon facility

R. Cywinski<sup>a,\*</sup>, A.E. Bungau<sup>a</sup>, M.W. Poole<sup>b</sup>, S. Smith<sup>b</sup>, P. Dalmás de Reotier<sup>c</sup>, R. Barlow<sup>d</sup>, R. Edgecock<sup>e</sup>, P.J.C. King<sup>e</sup>, J.S. Lord<sup>e</sup>, F.L. Pratt<sup>e</sup>, K.N. Clausen<sup>f</sup>, T. Shiroka<sup>g</sup>

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<sup>d</sup> School of Physics and Astronomy, University of Manchester, Manchester M13 9PL, UK

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### ARTICLE INFO

#### PACS

29.25.-t  
29.20.-c  
76.75.+i

#### Keywords

Stand-alone muon sources  
Non-scaling FFAG accelerators  
Muon spin spectroscopy

### ABSTRACT

We discuss possible designs for a high-intensity, stand-alone muon source dedicated to and fully optimised for  $\mu$ SR studies. In particular, we focus upon the potential implementation of a new generation of high-power, but relatively compact and cost effective, proton drivers based on non-scaling fixed-field alternating gradient (ns-FFAG) accelerator technology. Initial considerations suggest that a facility with multiple optimised pion targets, each affording positron count rates approximately two orders of magnitude higher than existing pulsed muon sources, together with the potential of steady state operation at count rates comparable to the best existing sources, should be achievable at reasonable cost. The relative merits of a stand-alone muon facility with respect to those of current facilities which operate in symbiotic mode with other users of the proton driver are highlighted. The outstanding technical issues which must be addressed by both muon scientists and accelerator technologists are also considered.

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### 1. Introduction

The production of high-intensity, spin-polarised muon beams is intrinsically related to the availability of secondary pion beams, the generation of which, in turn, requires the use of high-intensity proton accelerators. The high costs related to accelerator construction and operation have resulted in the so-called multi-purpose facility model, where muon, neutron and particle physics experiments are carried out at the same facility, typically running a medium energy (~800 MeV) accelerator.

This co-existence, at best symbiotic and at worst parasitic, was understandable in the early days of  $\mu$ SR, when the technique was still in its infancy and the user community rather small. However, the resulting paradigm is a compromise in which many muon beam parameters are far from optimal, thereby limiting the potential of the  $\mu$ SR method and often precluding developments which could be realised at a dedicated source.

Today, when  $\mu$ SR has a wide user base and is a well established and powerful tool in condensed matter science which complements, and in some cases competes with neutron scattering [1,2], there are good reasons to investigate other models of muon beam

delivery. Indeed there is a growing consensus that the concept of a stand-alone muon source is most certainly worth pursuing [3].

The current paper discusses possible designs for a high-intensity, stand-alone muon source dedicated and fully optimised for  $\mu$ SR studies of condensed matter. In particular, we shall focus upon the potential implementation of a new generation of high-power, but relatively compact and cost effective, proton drivers based on non-scaling fixed-field alternating gradient (ns-FFAG) accelerator technology.

### 2. Optimal proton driver parameters for a dedicated muon source

Any stand-alone muon facility must be based upon sufficiently flexible accelerator technology to afford optimal tuning of the proton driver parameters. The necessary requisites are considered in detail below and, to better illustrate the advantages offered by the new paradigm, we compare these requisites with the parameters of two representative muon sources: ISIS and PSI, operating in pulsed and continuous (CW) mode, respectively.

**Proton driver power and energy:** Both current European muon facilities have similar muon count rates ( $25\text{--}40 \times 10^3 \text{ s}^{-1}$ ). At a continuous source, as only one muon (with half life of 2.2  $\mu$ s) can be allowed in the sample at a time, the experimental (positron)

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A stand-alone optimised muon facility could deliver x100 intensity gains in pulsed mode and comparable intensity to PSI in CW mode

A 1Gev, 0.5mA Fixed Field Alternating Gradient proton accelerator at KHz frequencies would be an appropriate cost effective driver

Simulations of (multiple) pion/muon production targets and accelerator/target/collection/beam optics combinations are necessary

.....But first the codes have to be benchmarked  
- *against the ISIS target?*

.....could the ISIS target geometry/muon collection system be optimised as part of the same programme?

→ **GEANT 4**

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# GEANT4

Geant4 is a toolkit for the simulation of the passage of particles through matter

Developed and maintained at CERN

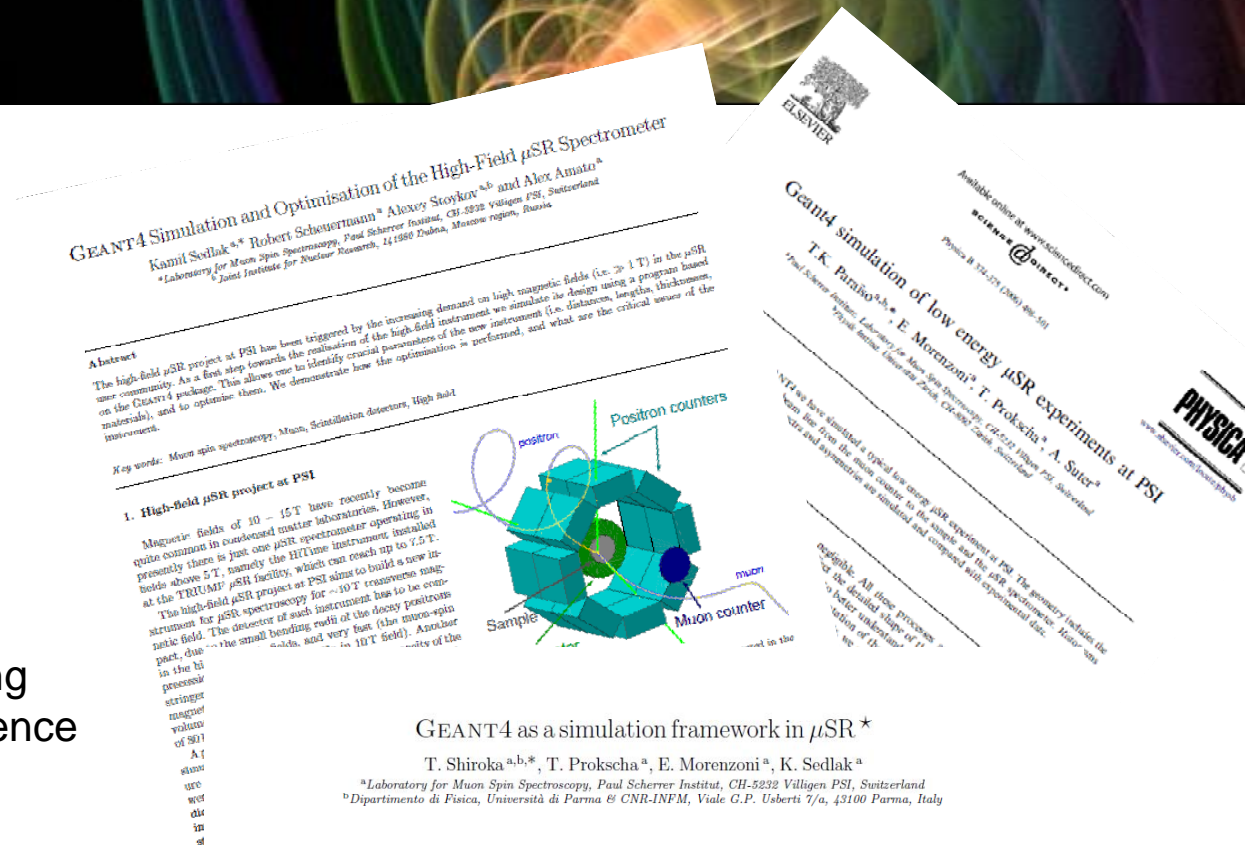
Originally intended for high energy physics experiments (eg LEP)

Now wide range of uses including medical, nuclear, and space science

Distributed as a set of C++ libraries

GEANT4 is already used in simulations of  $\mu$ SR experiments  
eg, Prokscha, Shiroka, Lancaster, Sedlak .....

Can GEANT4 accurately simulate proton/target interactions ?



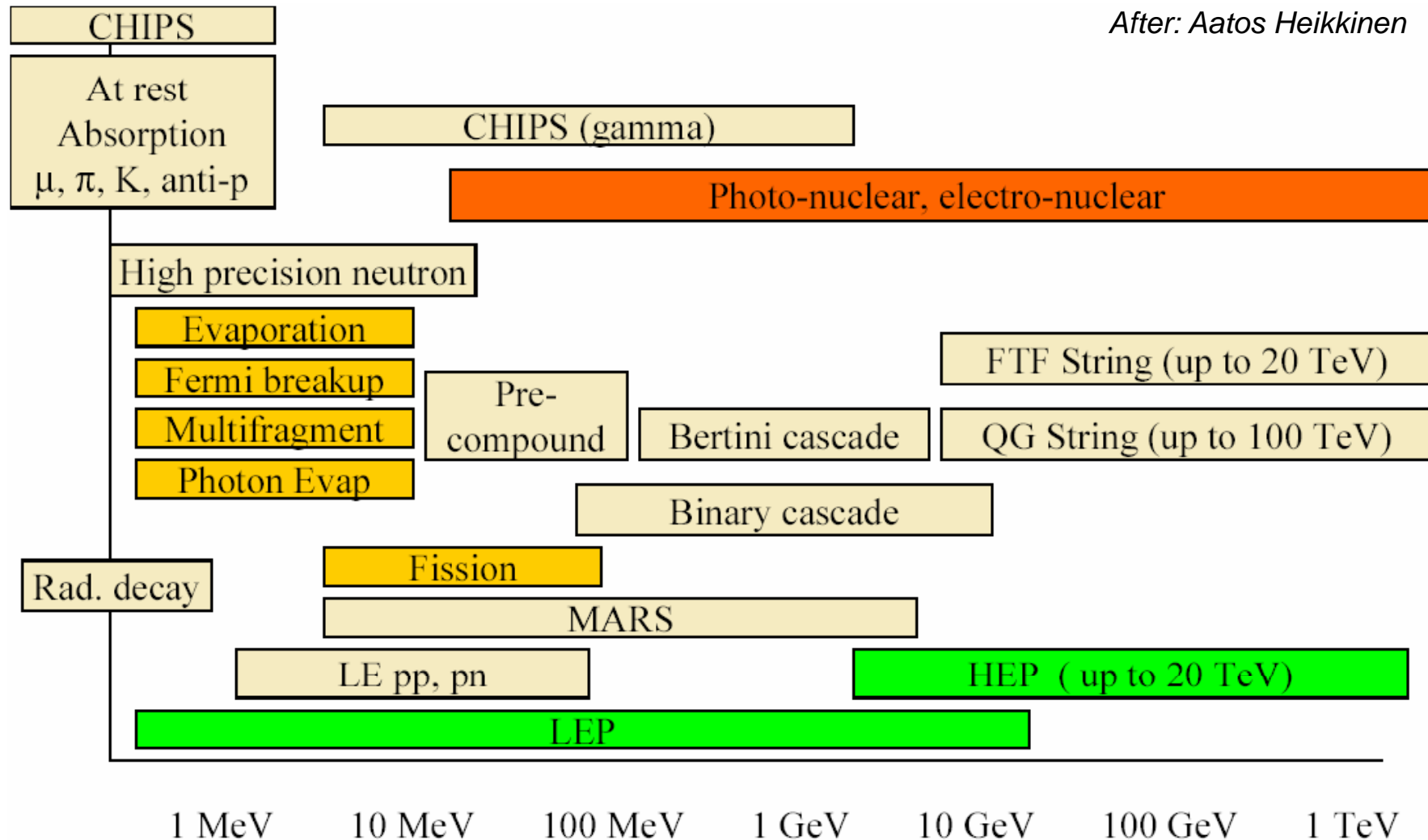
## 1. Introduction

The Monte Carlo method is a computer-based statistical sampling technique for solving complex, nonstandard problems. Due to its general-purpose, numerical approach the method has found a wide range of applications in many

which needs to accommodate more elaborate sample environments, the situation has changed. The growing demand to understand the detailed operation of muon spectrometers has been recognized by the FP6 JRAS program, where the development of software code to enable full instrument simulation has a dedicated work package.

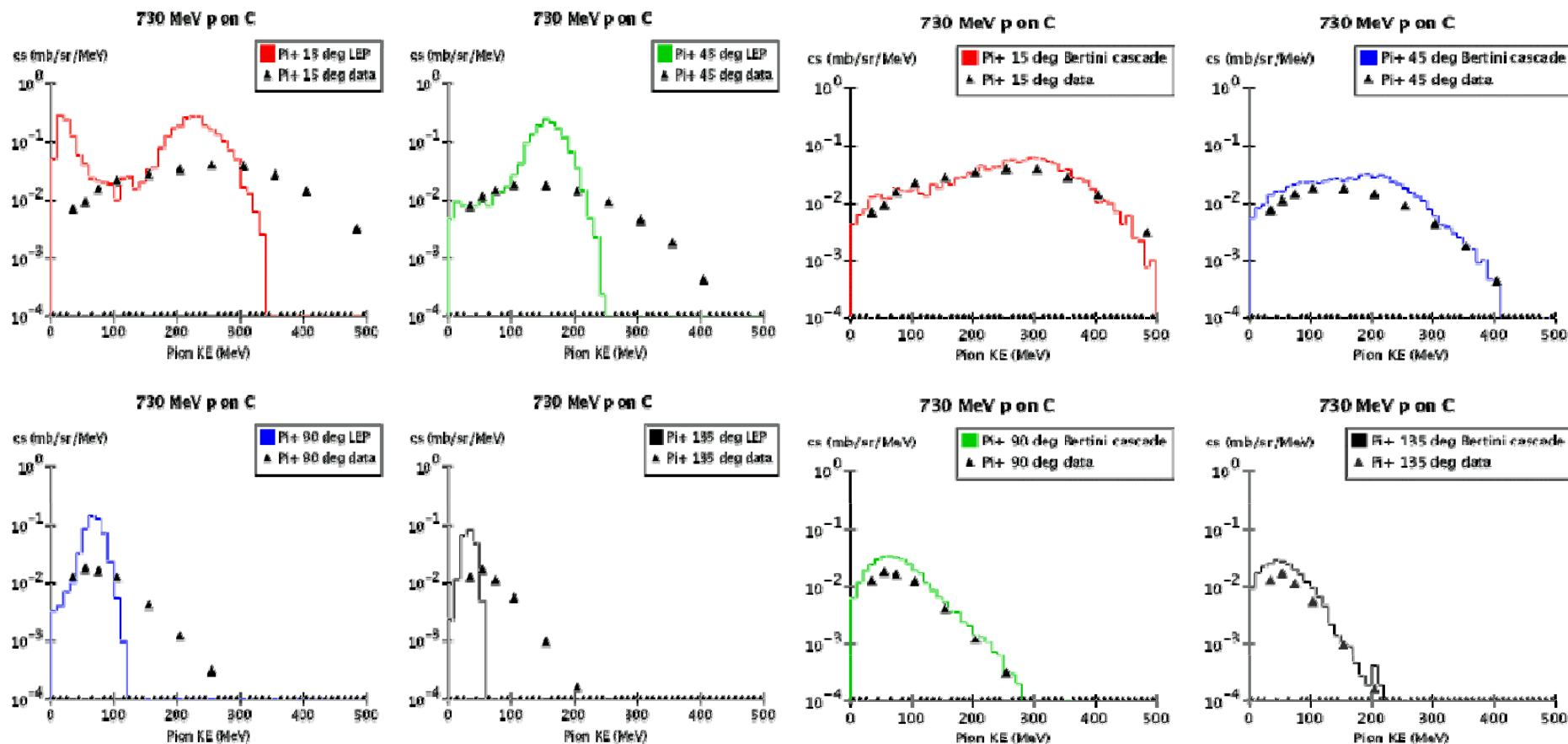
# GEANT4: hadronic model inventory

*After: Aatos Heikkinen*



# GEANT4: eg LEP vs Bertini

After: Aatos Heikkinen



*Geant3.21 based Geant4 LEP model pion production from 730 MeV proton on Carbon.*

*Bertini cascade model pion production from 730 MeV proton on Carbon.*



# The ISIS muon target

## Proton beam:

800MeV with  $\sim 1$ MeV energy spread

Focused to Gaussian “waist” at target with rms half width and rms half height of 5mm:

rms  $x'$  = 6mrad    rms  $y'$  = 5mrad

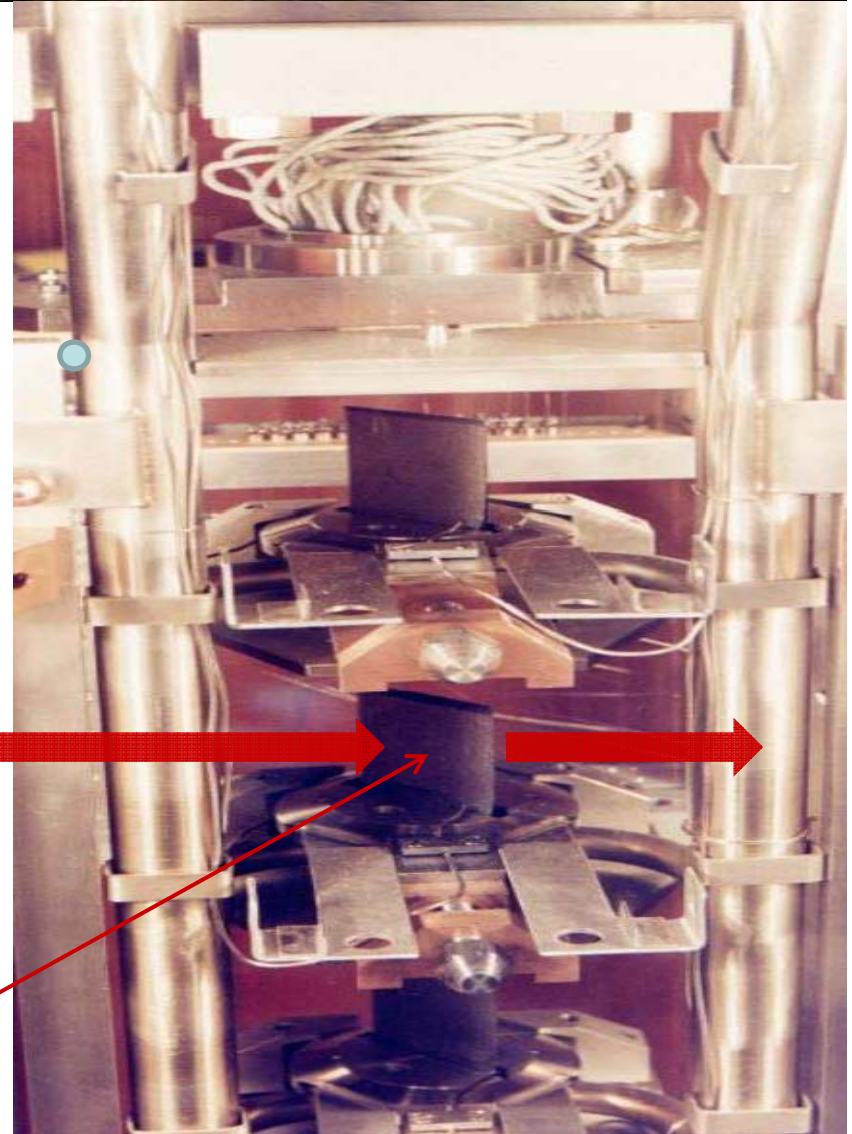
## Target:

Graphite plate 50\*50\*7 mm<sup>3</sup>

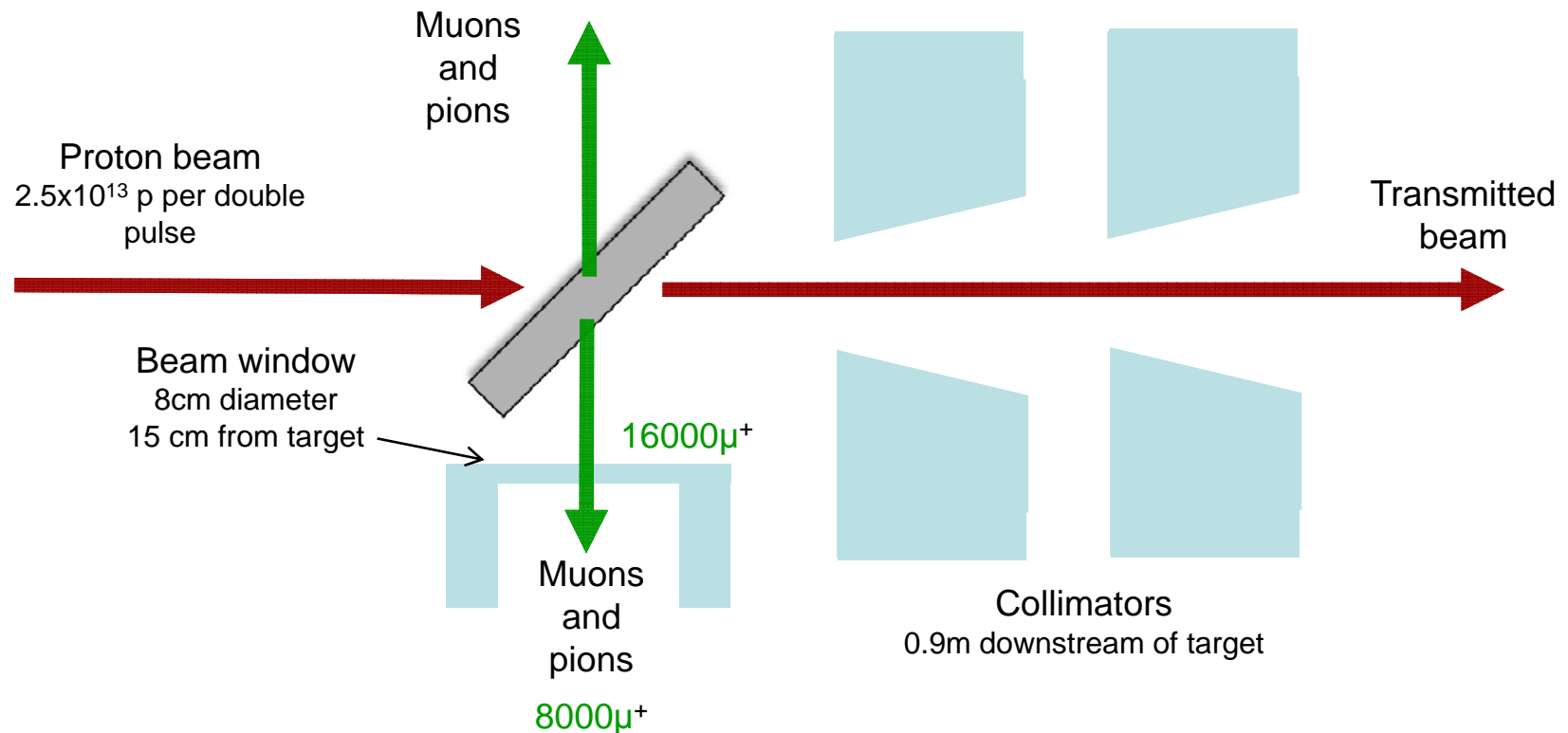
Oriented at 45° to proton beam (rotated around vertical axis)

Effective path length through target  $\sim 10$ mm

Graphite muon production target



# Simulation geometry



- Spatial cut:** (a) particles emerge from target within  $\pm 0.5\text{cm}$  vertically and  $\pm 3\text{cm}$  horizontally  
(b) particles must be parallel to beamline axis with  $180\text{mrad}$  in horizontal direction and  $35\text{ mrad}$  in vertical direction

**Momentum cut:** momentum bite must be between  $25.175$  and  $27.825\text{ MeV}/c$  (ie 10% around  $26.5\text{MeV}/c$ )

# GEANT4 simulations

GEANT4 and three physics models have been used:

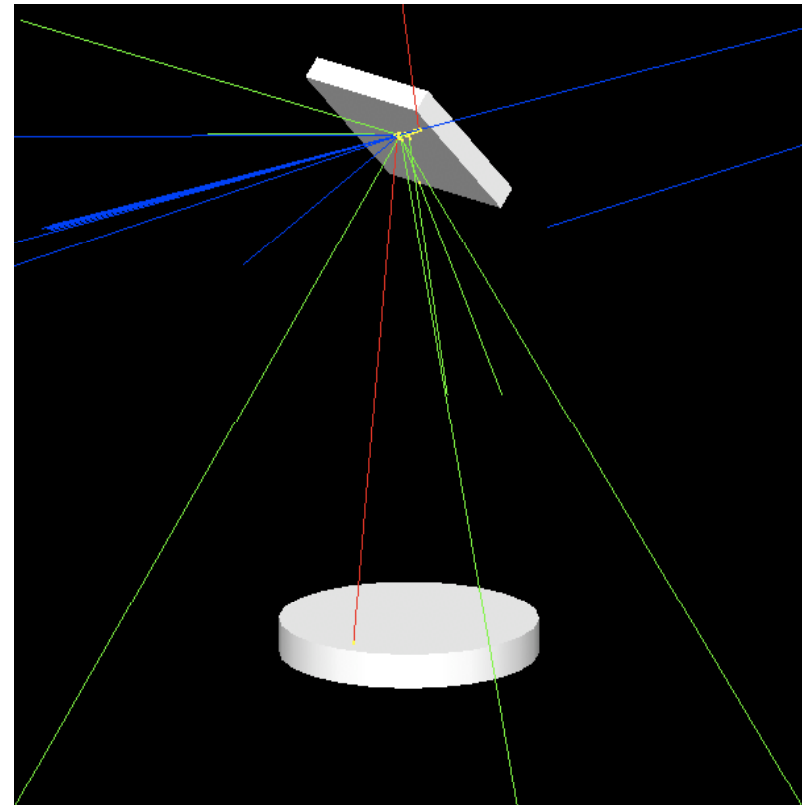
*Bertini model*

*Binary Cascade Model*

*INCL-ABLA model.*

Initial simulations of  $2 \times 10^{13}$  protons (corresponding to an ISIS double pulse) took a prohibitively long time to run

Shorter simulations of  $4 \times 10^7$  protons resulted in much poorer statistics, but in agreement with the longer runs and experiment, give the equivalent of 20000-40000  $\mu^+$  with the correct momentum and spatial cuts entering the beam window per ISIS double pulse.





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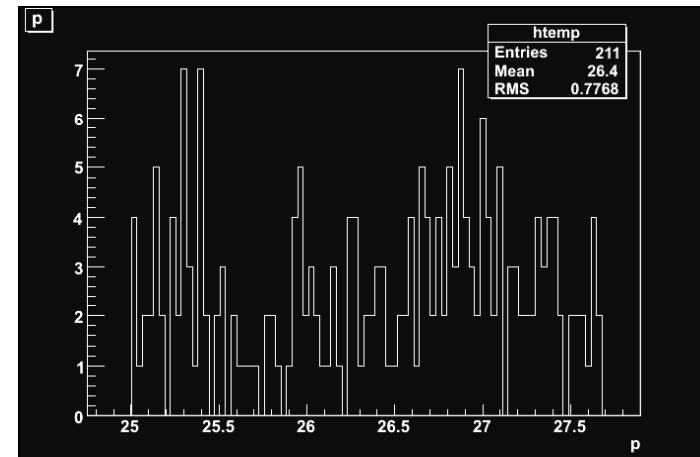
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*INCL-ABLA model.*

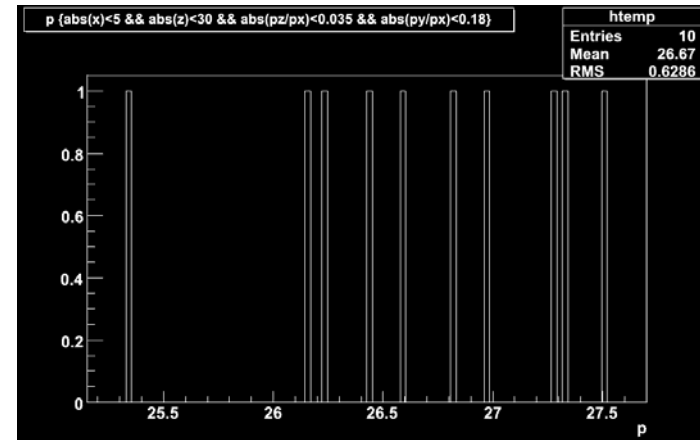
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The simulations showed a reasonably isotropic distribution of muons from the target – this was used to speed up the simulation procedures by separating pion production from muon transport



Momentum cut



Momentum, space and angle cut

# GEANT4 simulations

Each model generates the final state for hadron inelastic scattering by simulating the intra-nuclear cascade.

## *The Bertini model:*

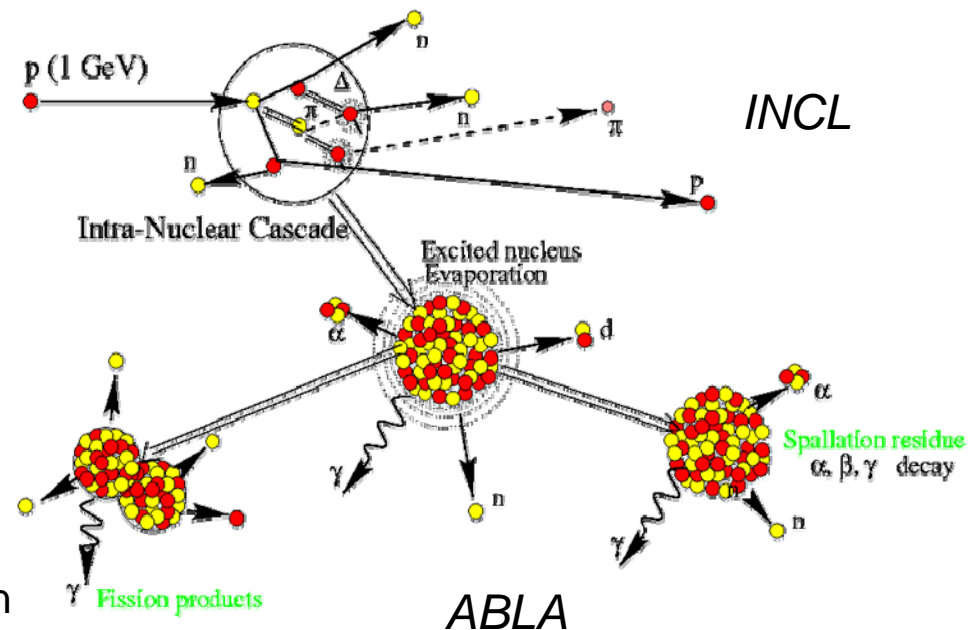
The target nucleus is treated as an average nuclear medium to which excitons (particle-hole states) are added after each collision.

## *The Binary Cascade model:*

The target nucleus is modelled by a 3-D collection of nucleons, as opposed to a smooth nuclear medium.

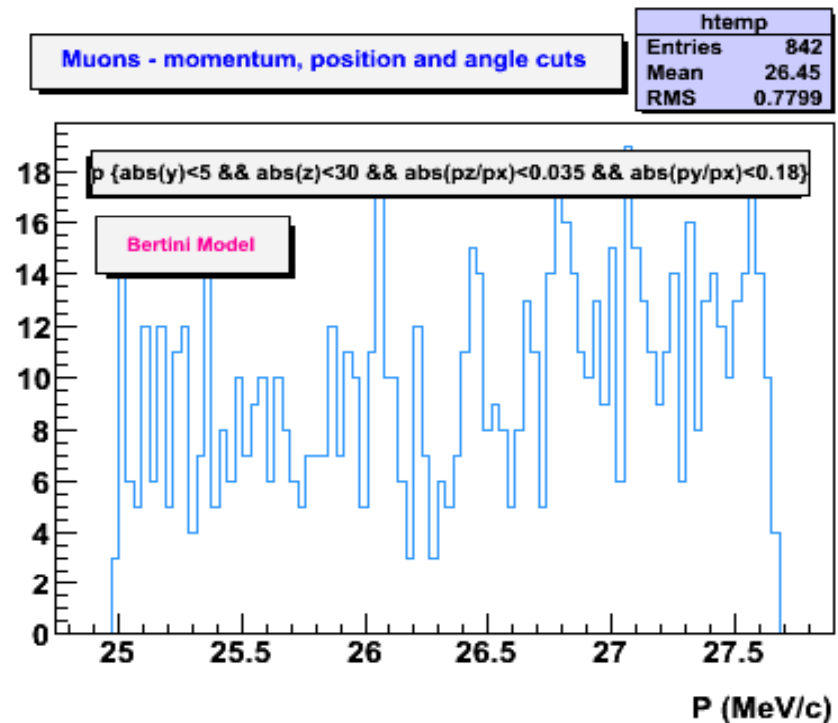
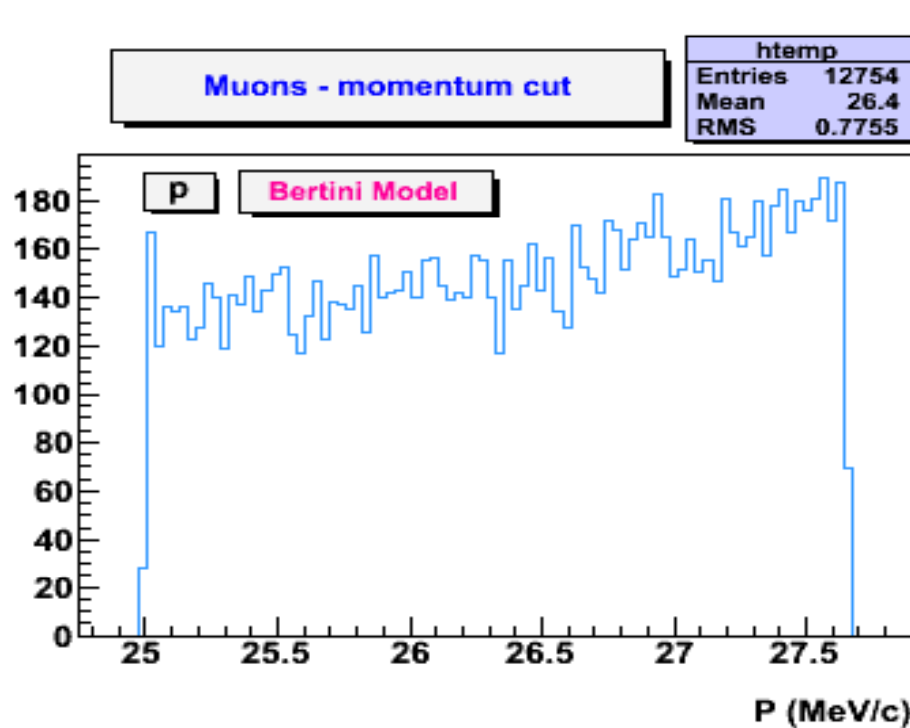
## *The INCL-ABLA model*

The intra nuclear cascade is based upon the Liege cascade model (INCL) and the de-excitation is based on ABLA



# Bertini Cascade Model

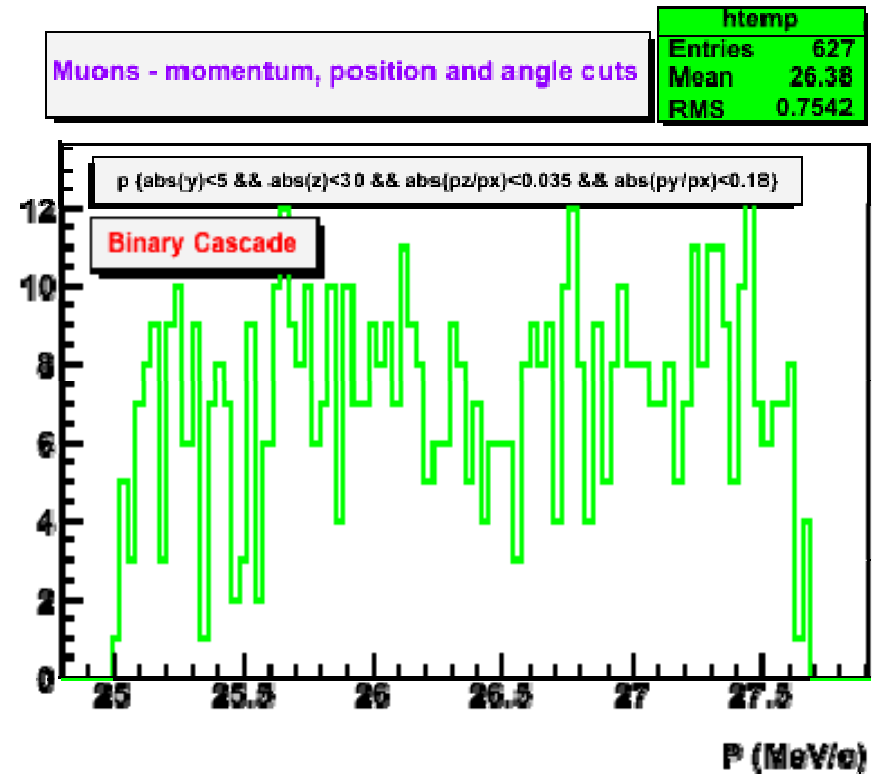
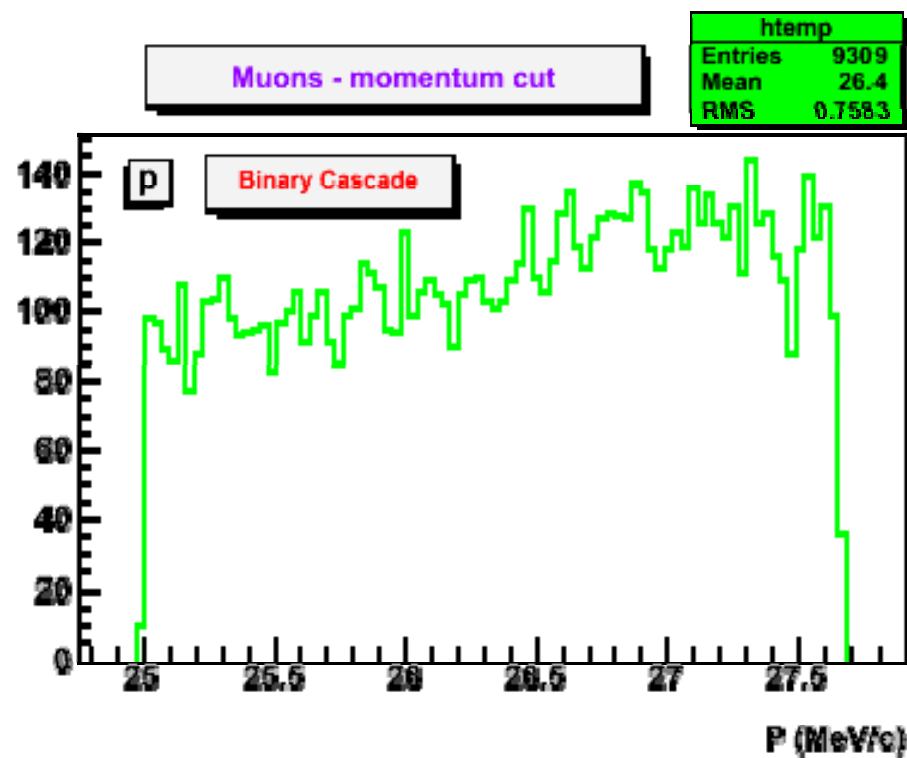
- simulations are for  $2.5 \times 10^{11}$  protons on target
- for  $2.5 \times 10^{13}$  protons there are **84200** positive muons entering the beam window





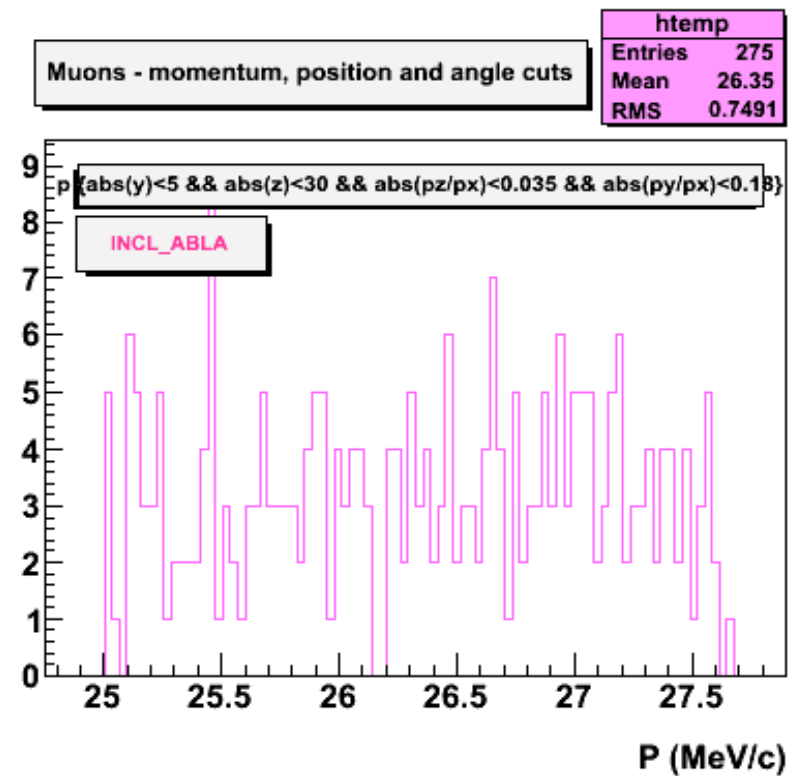
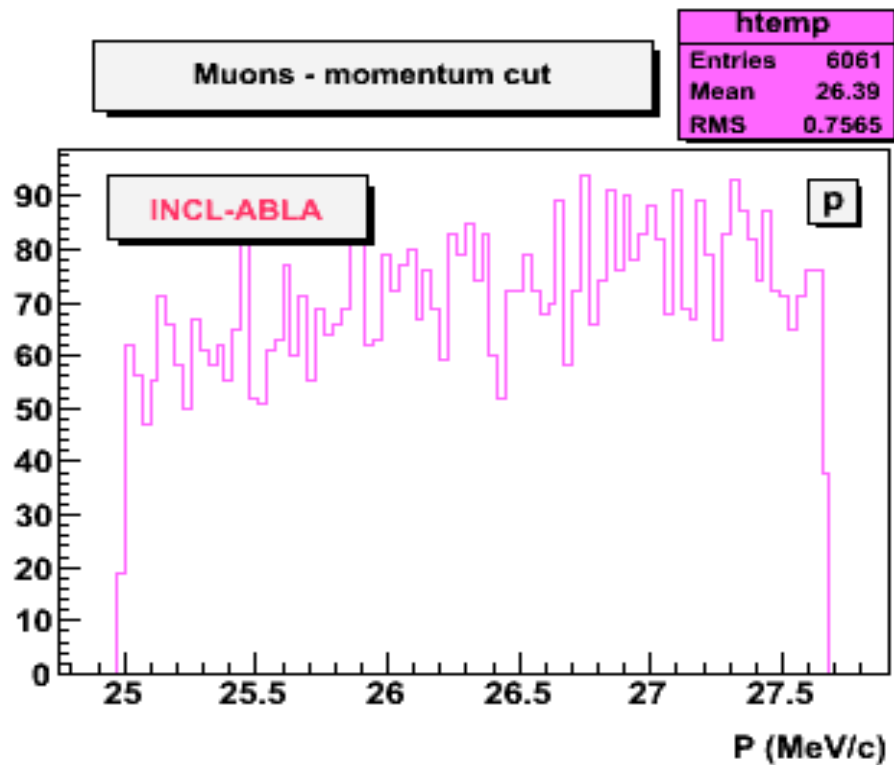
# Binary Cascade Model

- simulations are for  $2.5 \times 10^{11}$  protons on target
- for  $2.5 \times 10^{13}$  protons there are 62700 positive muons entering the beam window



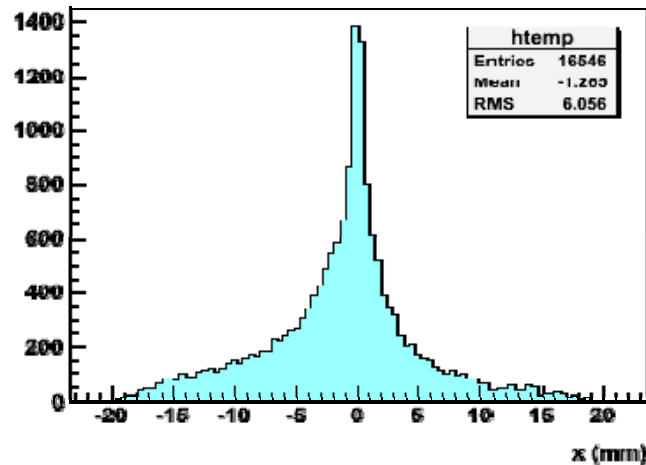
# INCL-ABLA Model

- simulations are for  $2.5 \times 10^{11}$  protons on target
- for  $2.5 \times 10^{13}$  protons there are **27500** positive muons entering the beam window

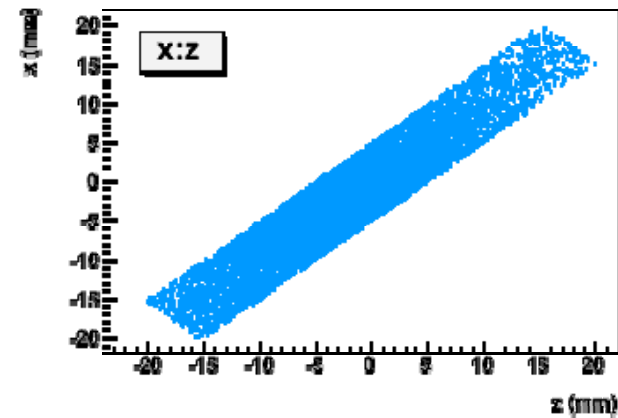


# INCL-ABLA: pions at rest in target

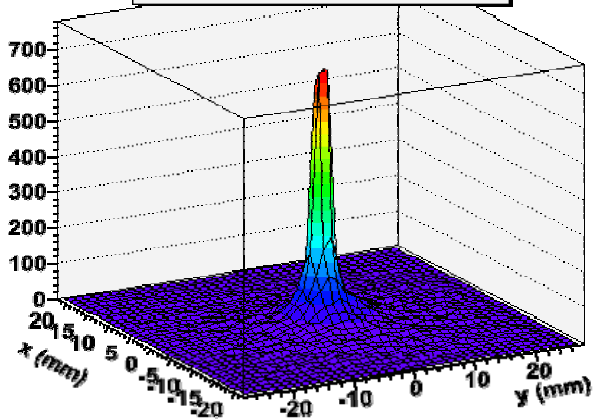
Distribution of pions at rest inside the target



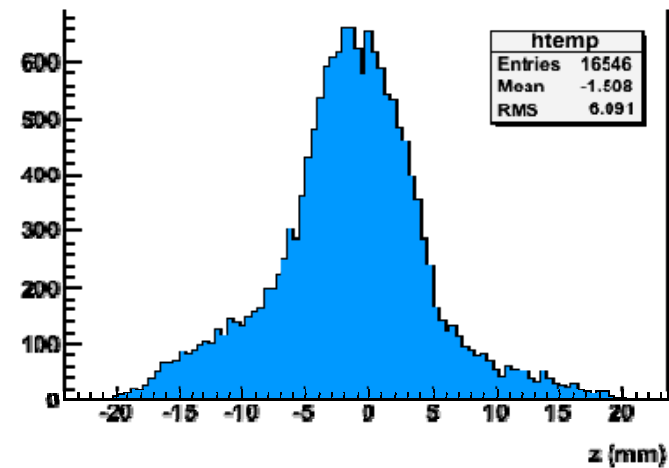
distribution of pions at rest inside the target - XZ plane



distribution of pions at rest in the XY plane



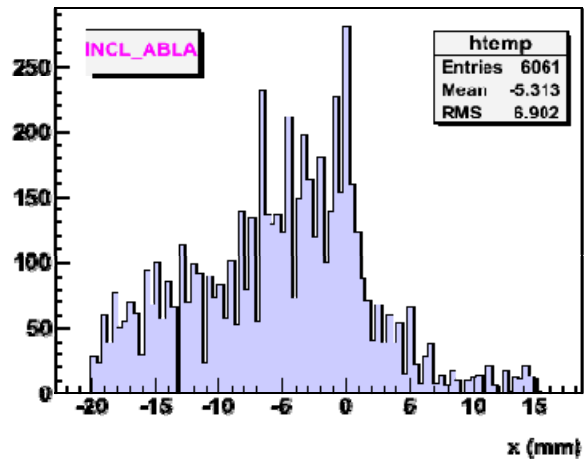
distribution of pions at rest inside the target



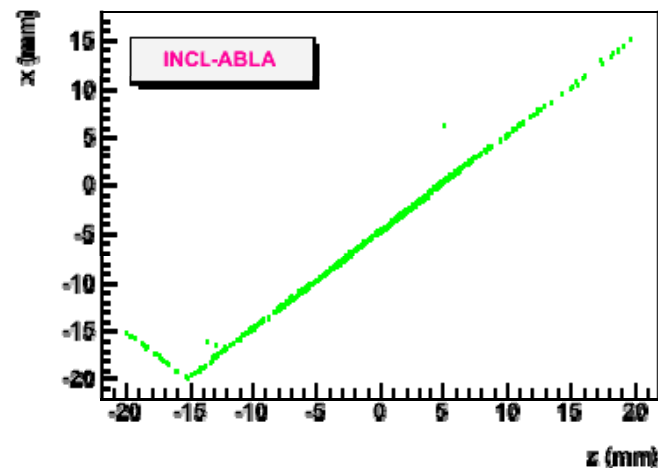


# INCL-ABLA: muon production

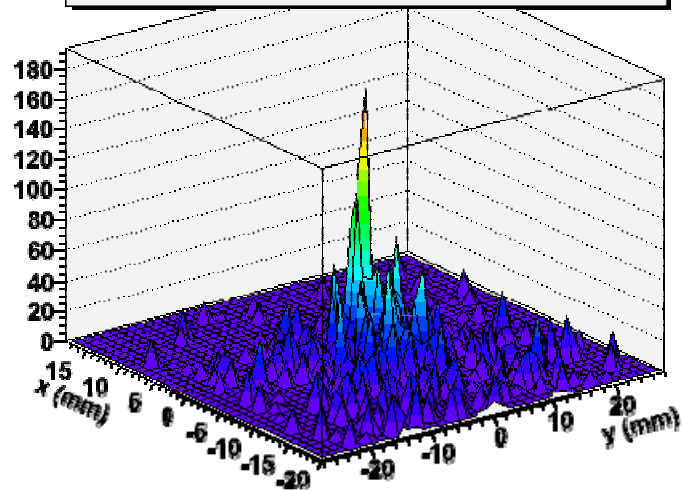
vertex position for muons inside the target



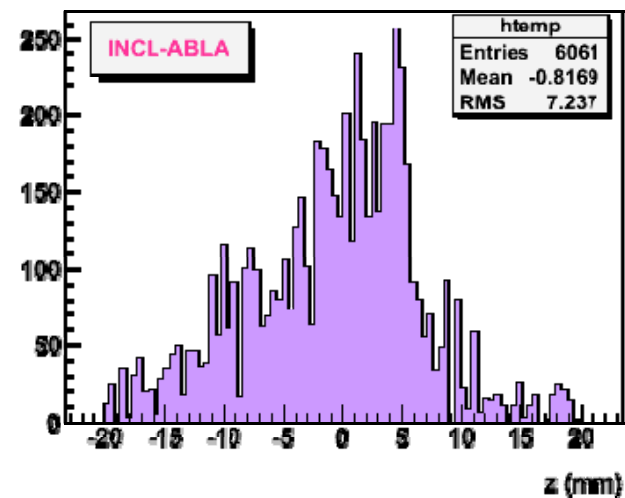
vertex position for surface muons - XZ plane



muons vertex position in XY plane - INCL-ABLA model

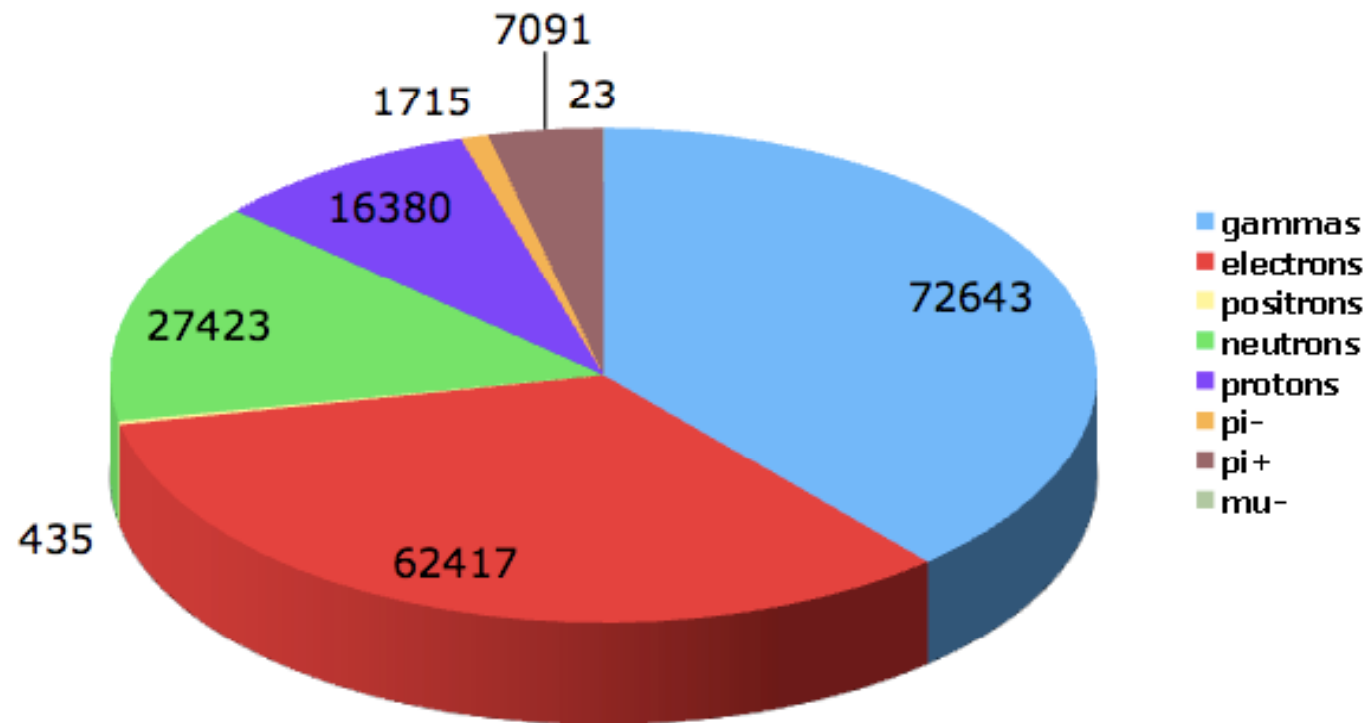


vertex position for muons inside the target

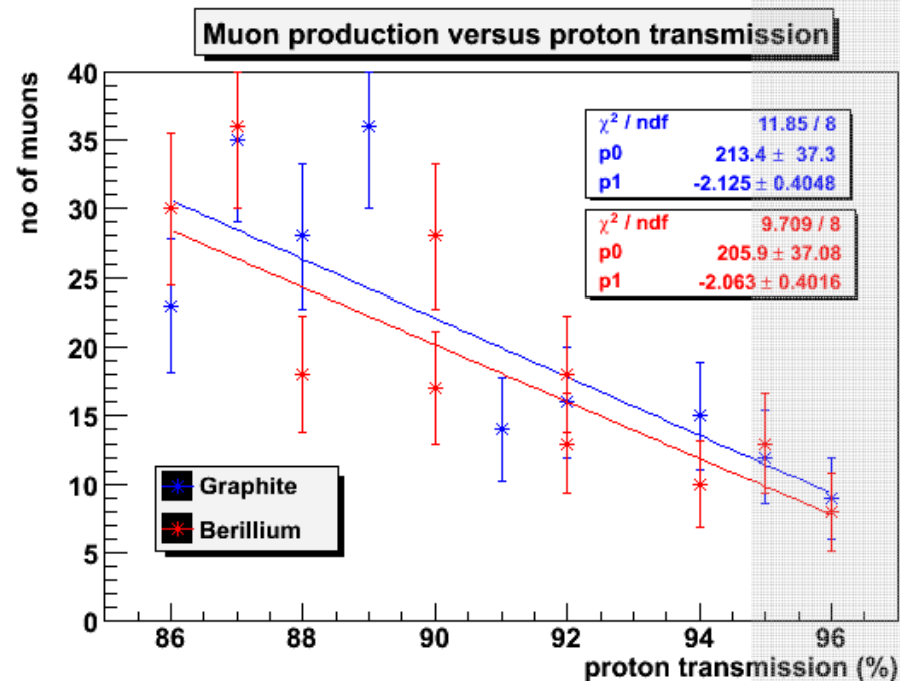
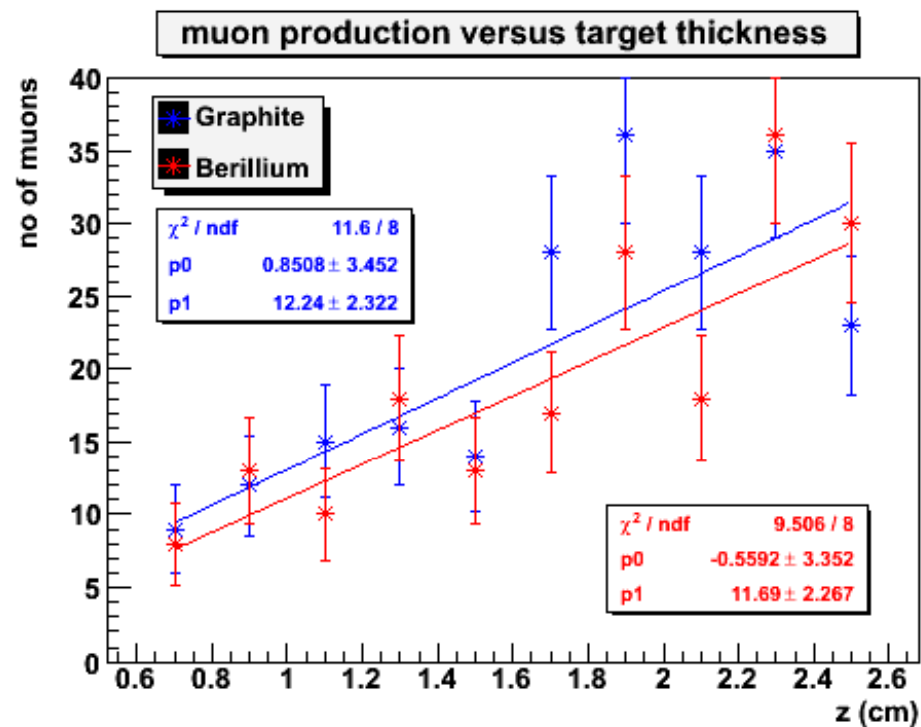


# Unwanted particles

Background particles entering the muon beam window



# Target material





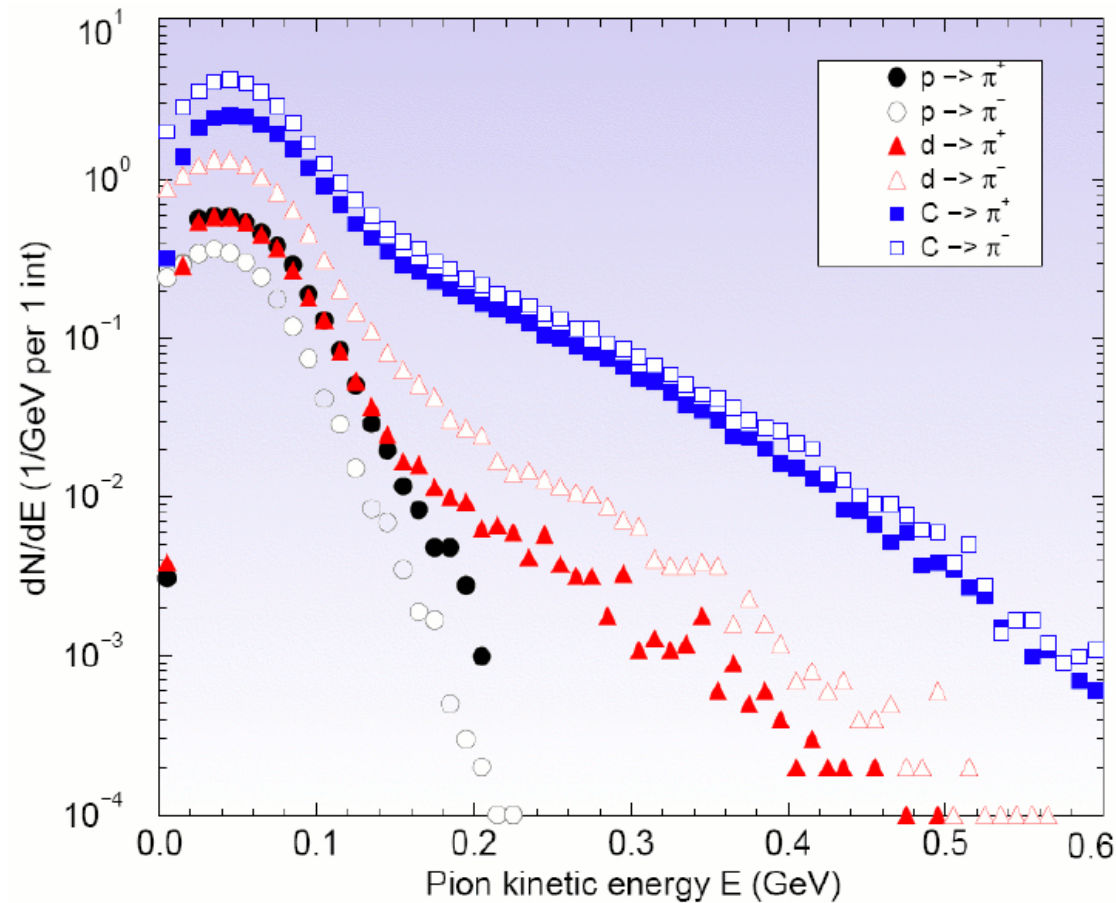
# Next steps

- ❖ Composite targets (eg Ni coated Be)
- ❖ Complex geometries (eg small xsection pencil/conical target)
- ❖ Proton loss calculations
- ❖ Thermal load calculations
- ❖ Improvement of collimators and collection geometries

With implications for

- ❖ Neutrino factory
- ❖ Stand-alone dedicated muon facility (protons?)

# Carbon ion beams



Pion spectra from 400 MeV/A projectiles on an **Hg** nucleus

Beam	$\pi^+$
p	0.0339
d	0.0337
C	<b>0.190</b>

Pion yield at  
 $30 < E < 230$  MeV

Carbon seems a  
promising projectile

*Simulations by N. Mokhov  
(From Shiroka)*