

# Numerical Simulation of $\mu$ SR Position-Sensitive Detectors

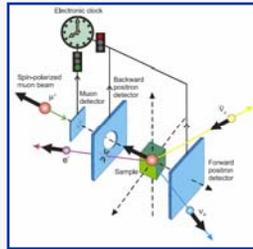
NMI3 Meeting  
Corsica, 27 June 2008

Toni Shiroka

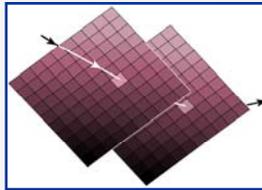
Laboratory for Muon-Spin Spectroscopy,  
Paul Scherrer Institut, Villigen, SWITZERLAND



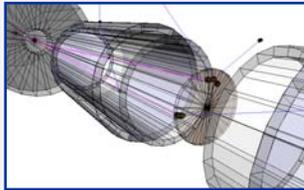
# Visual overview



Current limitations  
of the  $\mu$ SR technique



Position-sensitive  
detectors (PSD) for  $\mu$ SR



Numerical simulations as  
a test & optimisation tool

# Motivation: Extend $\mu$ SR to new domains

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- Current  $\mu$ SR relies on scintillation counting:  
scintillators – light guides – photomultipliers

## Advantages

- ✓ Fast response
- ✓ High detection efficiency
- ✓ High flexibility
- ✓ Inexpensive
- ✓ Etc...

## Not suitable with

- ✗ High magnetic fields
- ✗ Low-energy muons
- ✗ Tiny samples
- ✗ Etc...

## Objective

Development of **position-sensitive detectors** (PSD) and electronics readout based on new solid-state and integrated technologies – NMI3 JRA8

# PSD – New development ideas

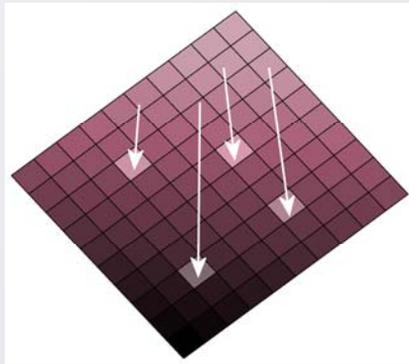
## Problem

- ▶ Pile-up effects
- ▶ Small samples / high backgr.
- ▶ High magnetic fields

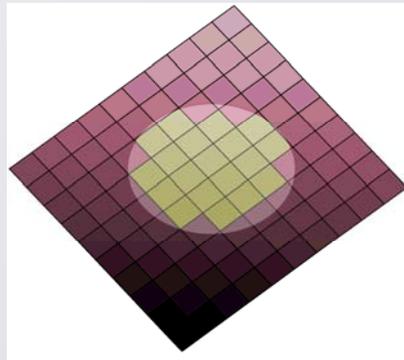
## Proposed solution

- ➔ Detector segmentation
- ➔ Particle origin reconstruction
- ➔ Segmentation / tracking

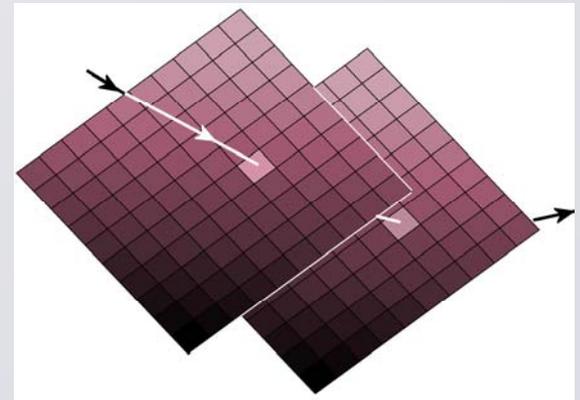
**Requirements:** High spatial resolution (1 mm or better)  
High positron detection efficiency (> 95%)  
Good time resolution (1 ns or better)



Pixel detector  
for count splitting



Software defined  
pixel geometry



Full particle  
tracking ?

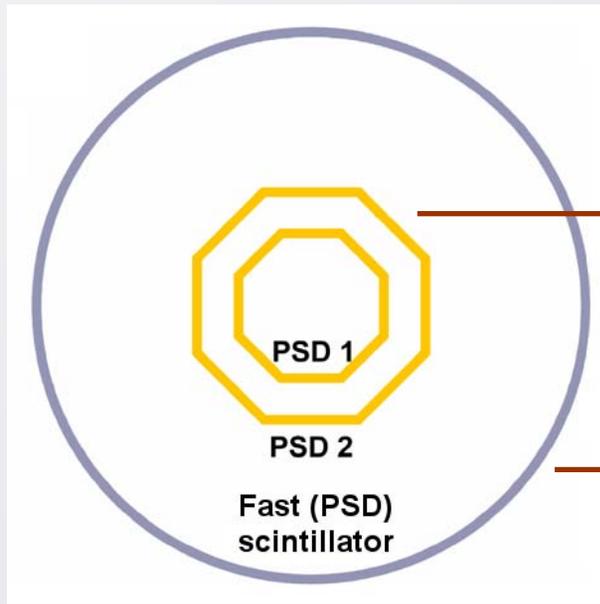
# Possible detector layout: Physics

**Mixed type** detectors successfully used in: NA58, FAROS, etc.

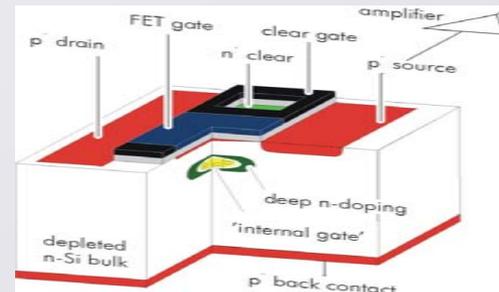
Detector = Silicon devices (position) + Scintillating fibres (timing)



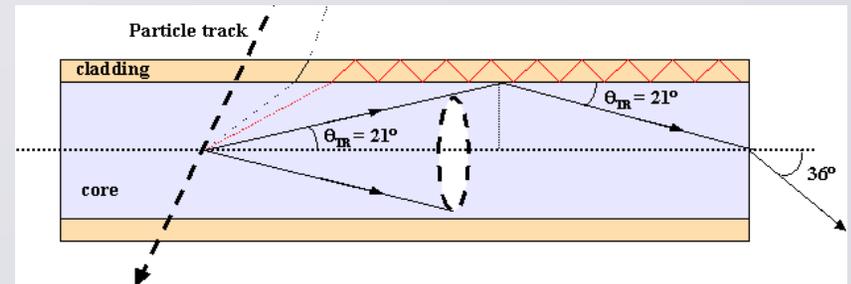
Improved overall performance due to **complementary advantages**



PS detector layout



Silicon  
DEPFET



Scintillating fibre - SciFi

# Exploring PSD using simulations

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Real tests: complex and difficult → Use simulations to **establish** and **optimize** preliminary detector performance

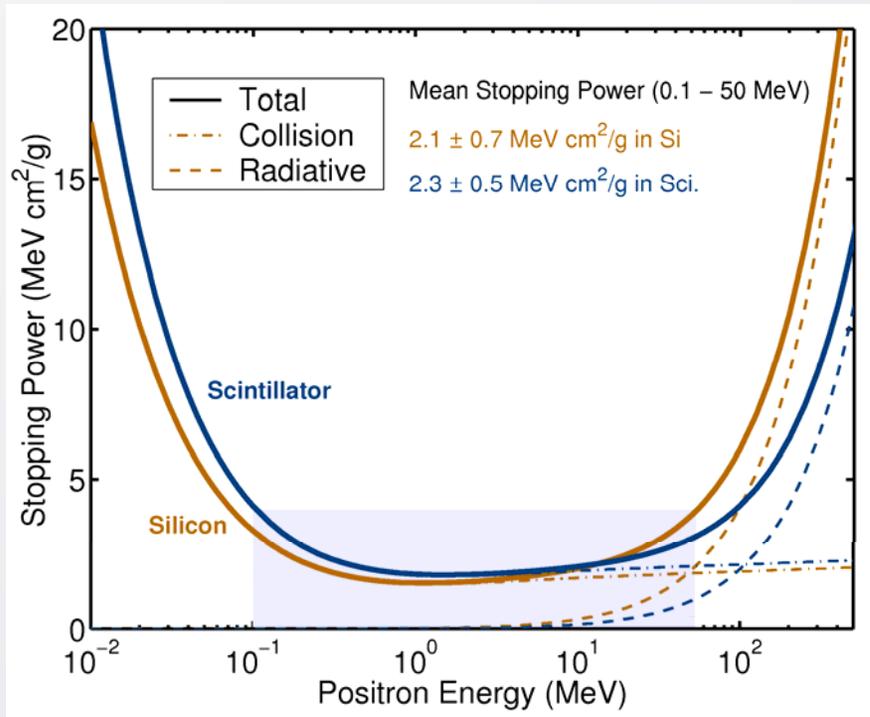
## Establish detector limits

- Muons  
Longitudinal and radial ranges, dispersion
- Positrons  
Exit fraction, energies, angle & coord. dispersion

## Optimize performance

- Parameter optimization  
Detector number, thickness, angles, distances, extension, position, pixel size, etc.

# Peculiarities of decay positrons



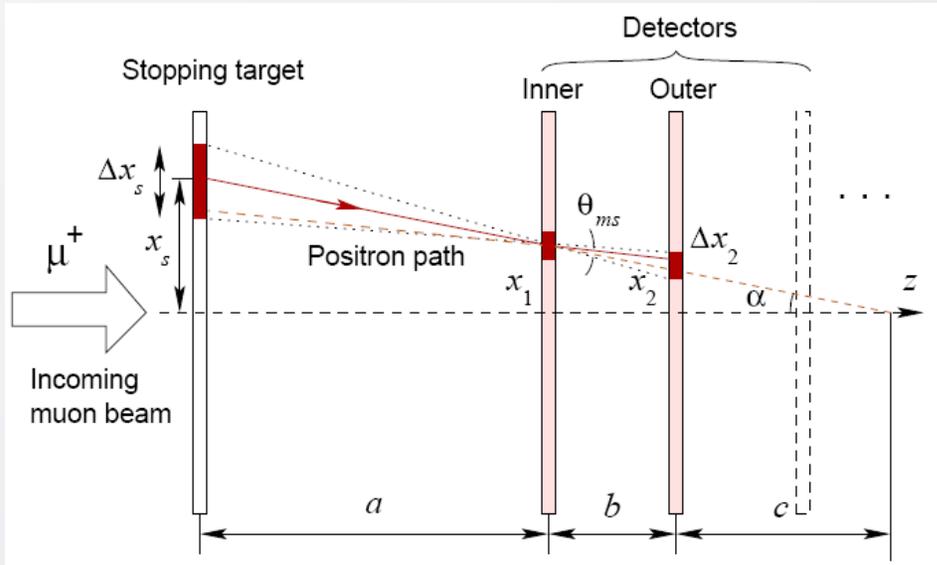
Stopping power vs. positron energy  
in silicon and scintillating fibres

Positrons in  $\mu^+$  decay:

- $T = 37 \pm 11$  MeV, much different from particles in colliders ( $T \sim 1$  GeV)  
➔ **large multi. scattering**
- Behave as minimum ionising particles (MIPs)  
➔ **low signal levels**
- Radiation level is low  
➔ **very limited damage**

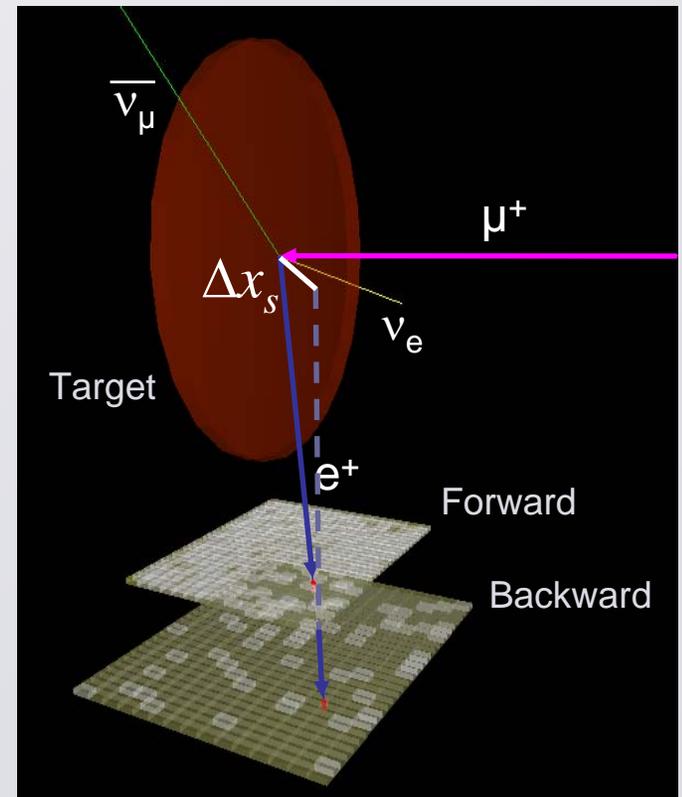
<http://physics.nist.gov/PhysRefData/>

# PSD Simulation method

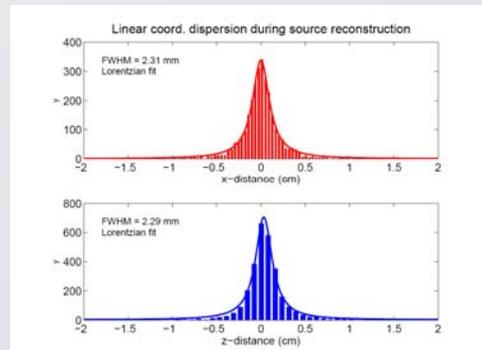


Detector schematics and ...

... GEANT4 Simulation



Statistical analysis



# Theoretical uncertainty predictions

Simplified case:  $\Delta x_p = 0$  (no pixel structure)

$$\Delta x_s = a \cdot \theta \cdot 1/\cos^2\alpha$$

Distance    Mult. Scatt.    Position & extension    **No** dependence on  $b$ !

Real case:  $\Delta x_p > 0$  (with pixel structure)

$$\Delta x_s = [(a/b+1)^2 \cdot \Delta x_{1p}^2 + (a/b)^2 \cdot (b^2 \theta^2 / \cos^4\alpha + \Delta x_{2p}^2)]^{1/2}$$

← Dependence on  $b$

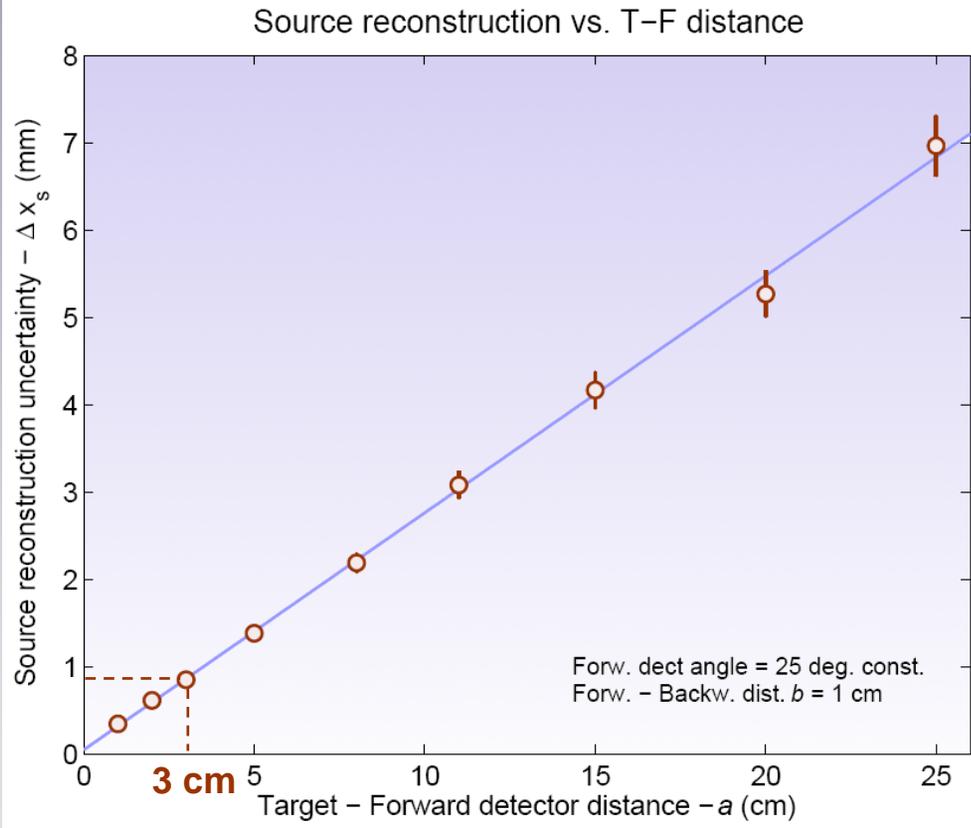
$$\Delta x_2 = [\Delta x_{2p}^2 + (b \cdot \theta \cdot 1/\cos^2\alpha)^2]^{1/2}$$

Pixel error

Mult. Scatt.

What do **simulations** predict ?

# Detector-to-target distance effect

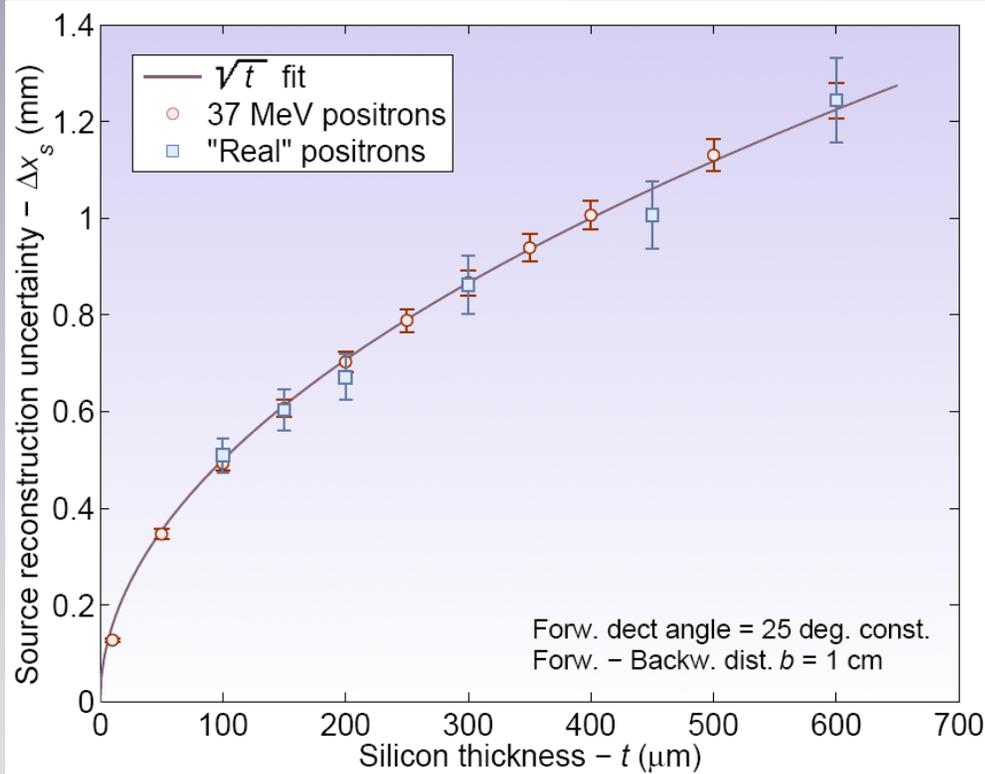


A linear error is expected with the first detector-to-source distance:

$$\Delta x_s = a \cdot \theta \cdot 1/\cos^2\alpha$$

**Conclusion:** Put the first detector as **closely** as possible to the target!

# Multiple scattering (thickness) effect



An increased error expected for thicker detectors, with large multiple scattering:

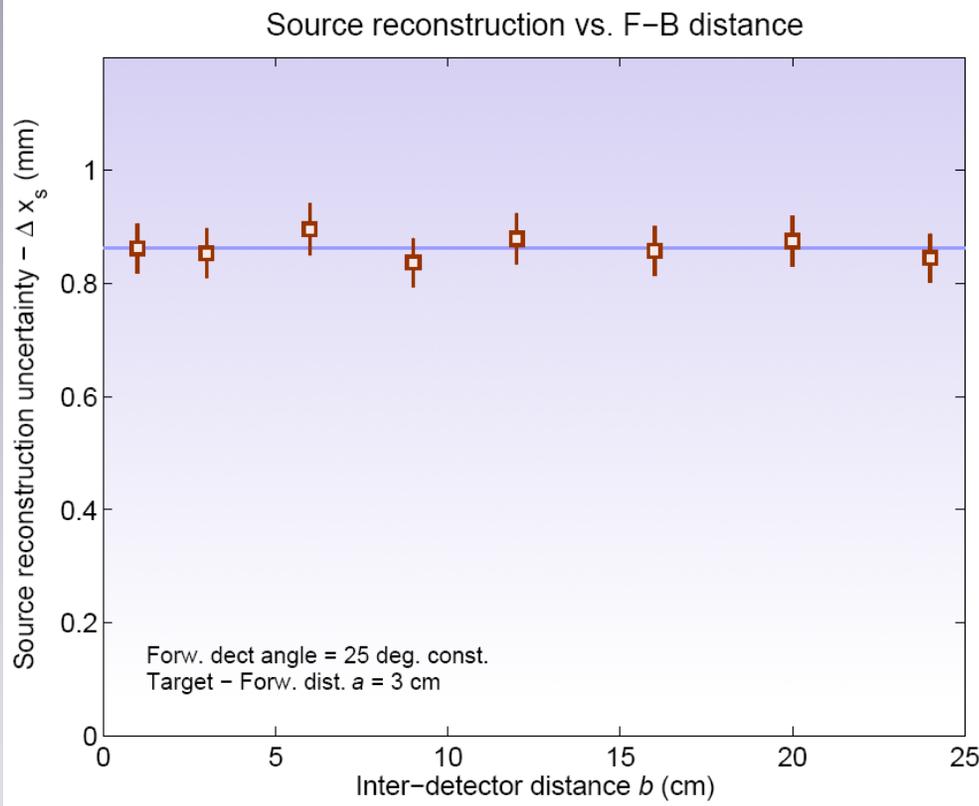
$$\theta \sim \sqrt{t}$$

$$\text{If: } \Delta x_s = a \cdot \theta \cdot 1/\cos^2\alpha$$

←  $\Delta x_s \sim \sqrt{t}$

**Conclusion:** Use a detector as **thin** as possible ( $\sim 300 \mu\text{m}$ ) compatibly with the S/N level

# Inter-detector distance effect



If the inner detector has no pixel structure a constant error with F-B dist. expected:

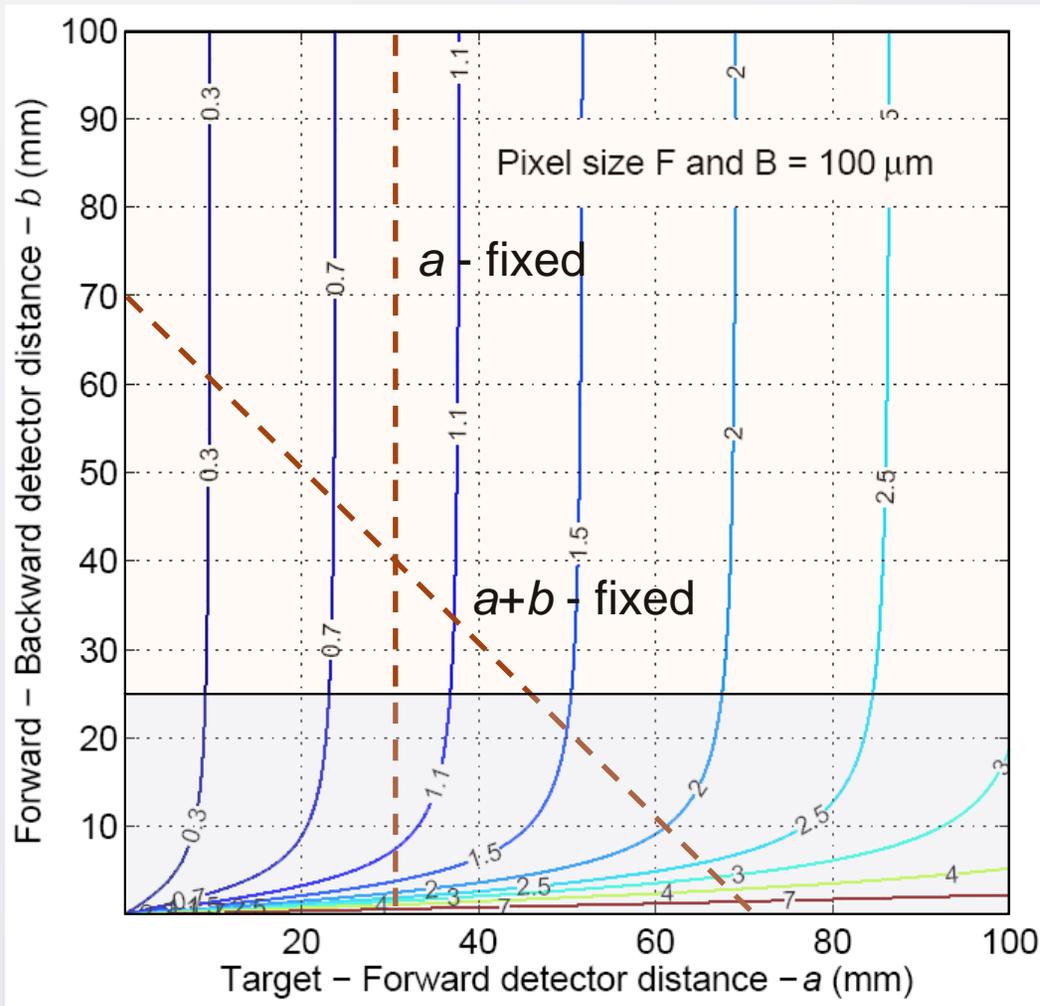
$$\Delta x_s = a \cdot \theta \cdot 1/\cos^2\alpha$$

**Conclusion:** Calculate errors also for a **pixelated** detector!



# 2D uncertainty map (Pixel size > 0)

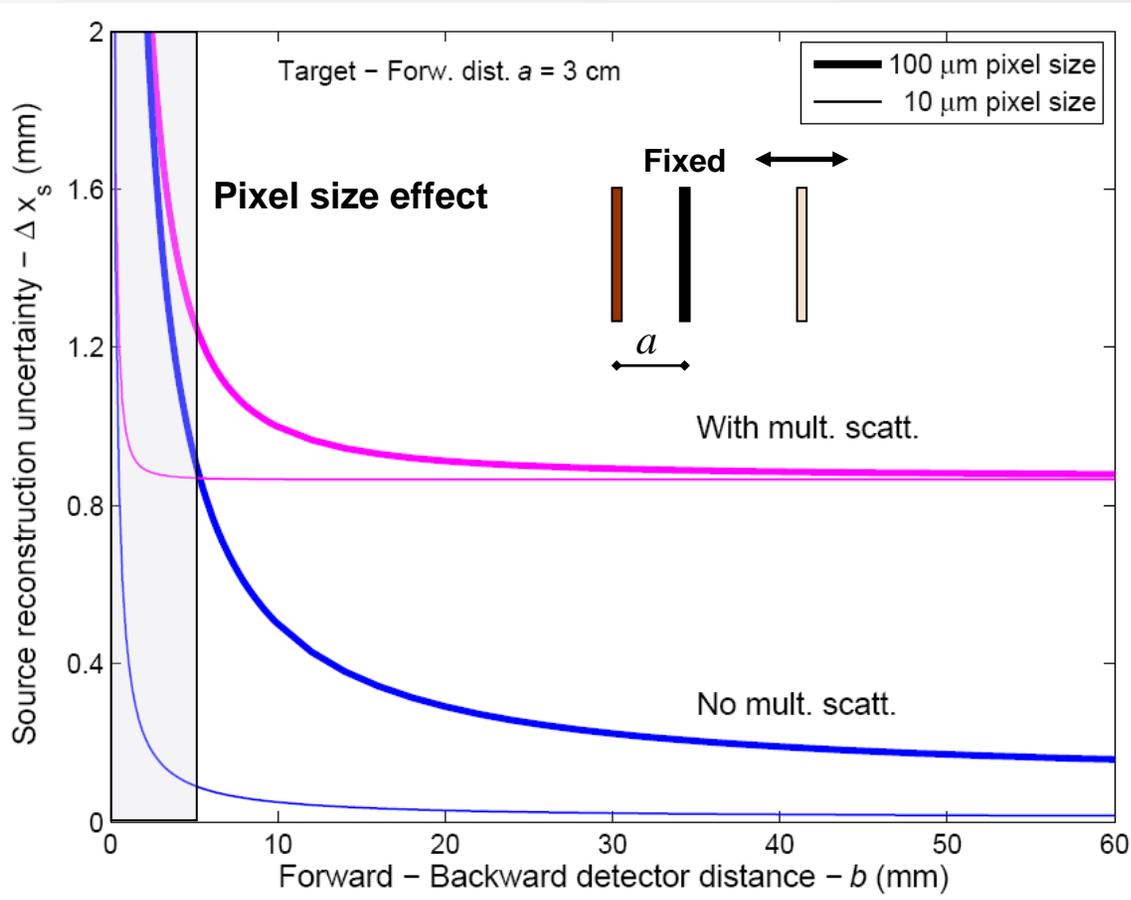
Source location error vs.  $a$  and  $b$  distances



Errors due to  
**Multiple scattering**

Errors due to  
**Finite PIXEL size**

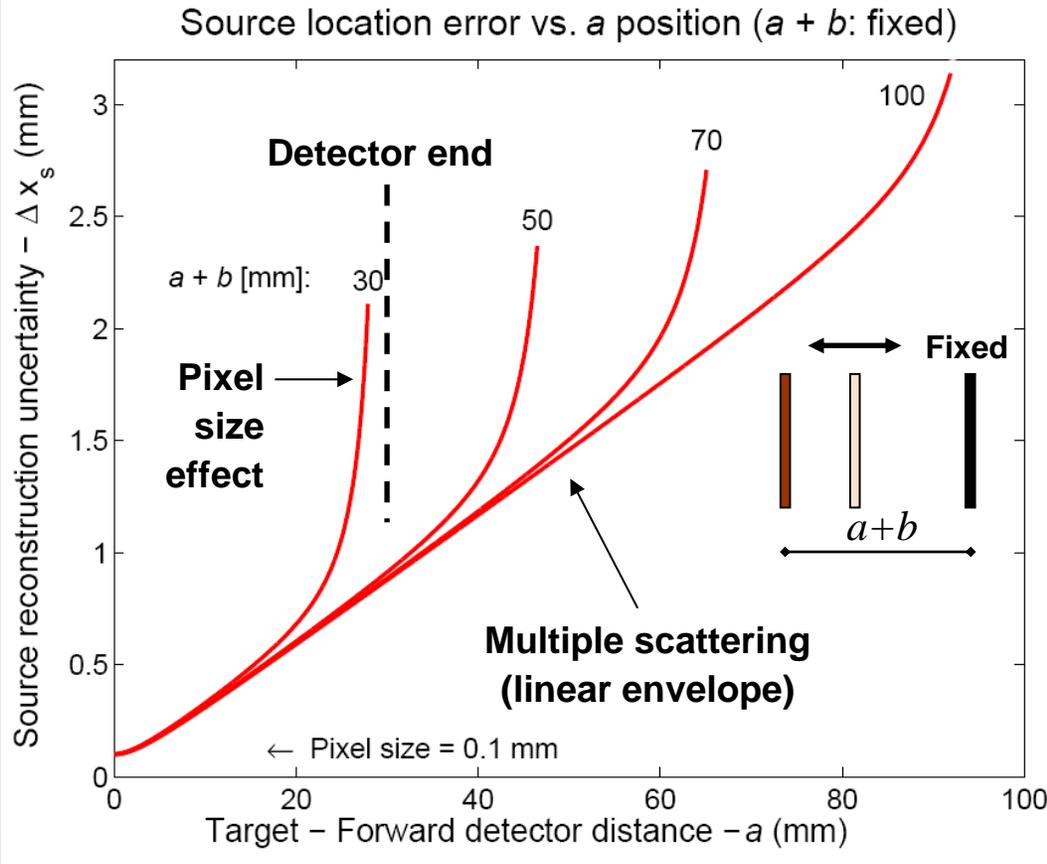
# Source reconstruction error: fixed $a$



- Multiple scattering is **unavoidable**. Big detectors won't improve resolution
- Pixel errors very important at **short distances**. Small pixels allow for a smaller detector
- At large distances, the error is **constant** and **independent** of pixel size

$a = \text{const}$ : mimics a fixed inner detector position

# Source reconstruction: fixed $a + b$



- **No position** can overcome the intrinsic pixel size error
- An **acceptable error** is found for  $a \sim b$  or less. Best solution for  $a \sim 0$ .

$a + b = \text{const}$ : mimics the limited space available for the detector

# Conclusions and future work

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- Detector **simulation** is crucial in optimizing detector performance and guiding the building of prototypes:
  - Critical** param.: Detector thickness, extension, distance to target
  - Important** param.: Pixel size, inter-distance, number of layers
- The desired resolution ( $\sim 1$  mm) is **achievable**. Further improvements are **limited** by intrinsic effects

## Future work

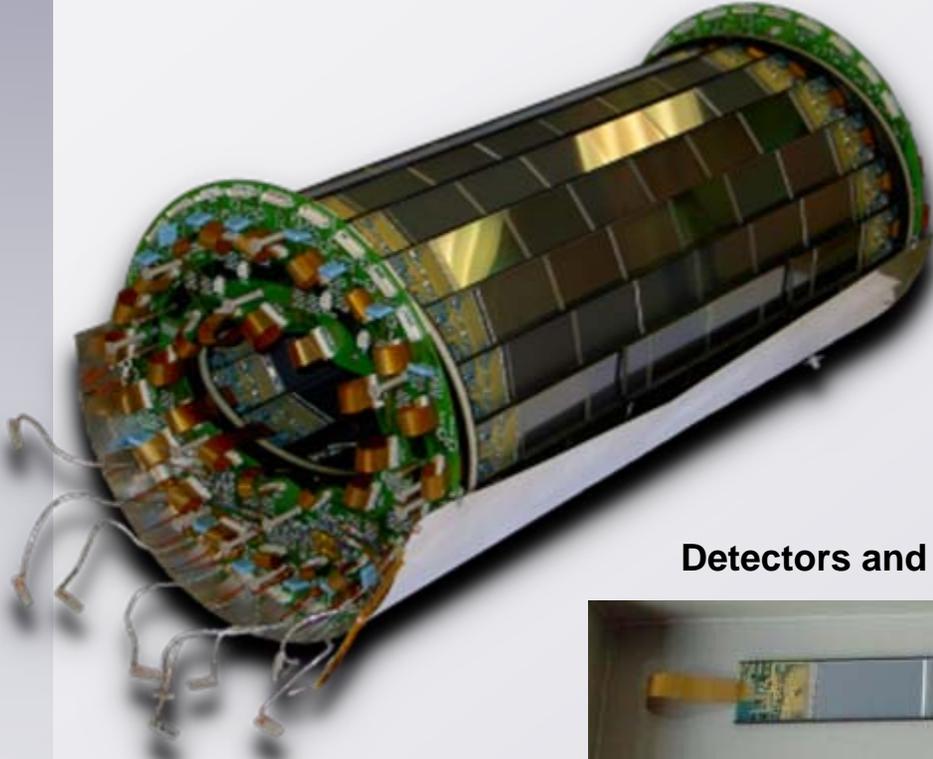
- **Testing of prototypes**: assess position sensing capabilities and timing in realistic conditions

# Simulation testing

H1 CST – silicon detectors

# H1 CST: HERA Central Silicon Tracker

Overall detector view



Top view of front-ends



Detectors and front-ends



One ladder: →  
6 double sided sensors  
+ 2 hybrid front-ends

# H1 CST detector: features and plans

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## Main detector features:

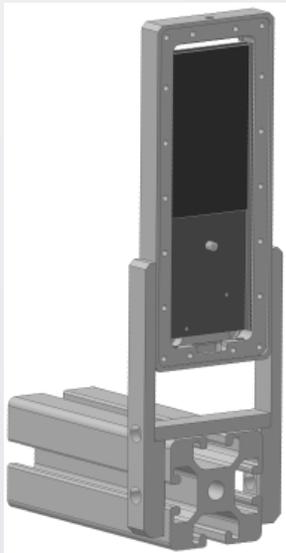
- 34 mm x 59 mm x **300  $\mu\text{m}$**  ( $0.3X_0$ )  
*double sided p-n sensors*
- **12  $\mu\text{m}$  strips**: 25  $\mu\text{m}$  pitch on  $p$  side and 88  $\mu\text{m}$  pitch on  $n$  side
- 37  $\mu\text{m}$  impact parameter resol.
- 640 readout lines per side
- **10 MHz** speed (100 ns rise time)
- 32 channel – PRO/A ASIC
- On-board preamp/shaper/discrim.
- Four step adjustable gain
- 2 l/min water cooling

## Timetable:

- Check for good modules
- Assembly the test detector
- Test air or water **cooling**
- Write MIDAS DAQ software
- Data collection and analysis
- Development of  $\mu^+$  beam monitor?

# PSD Performance testing

**PS detector holder  
(light-tight & cooled)**



**New data acquisition control system  
(Etrax – Altera Cyclone FPGA)**



**Solid-state Si pixel detector  
(adapted from HERA H1 CST)**

# Acknowledgements

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## People:

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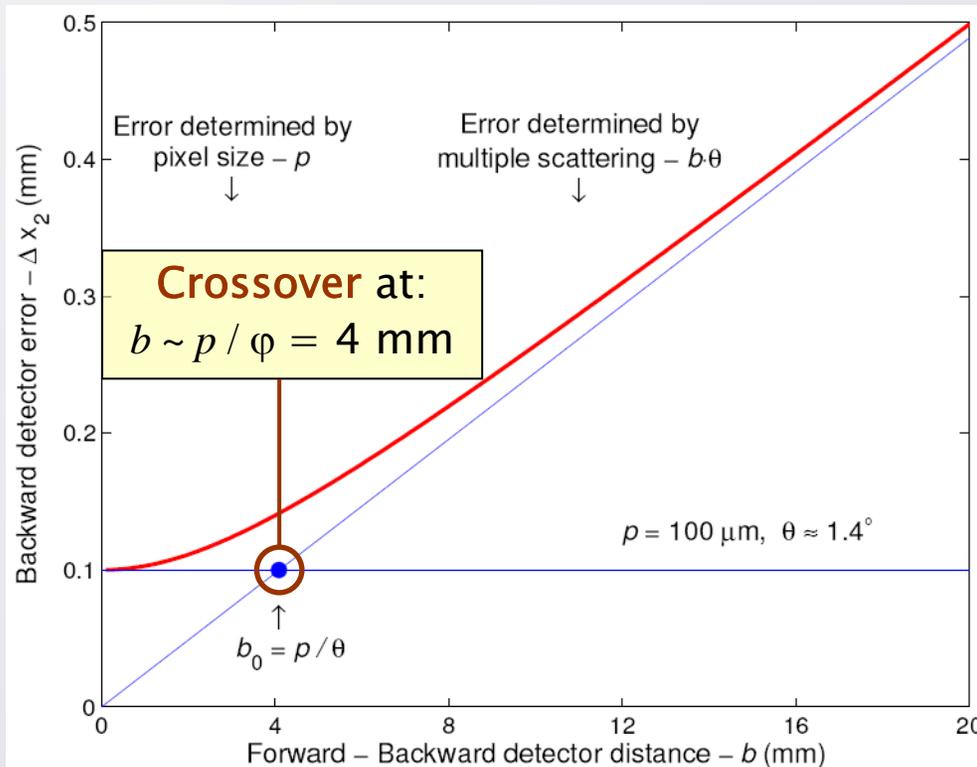


# Linear error in backward detector

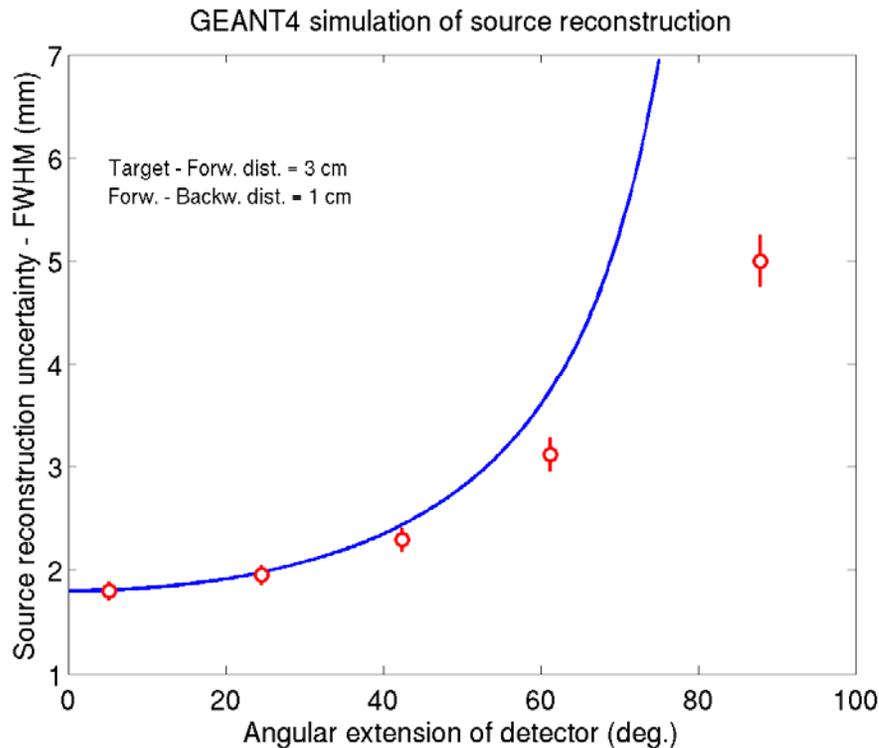
$$\Delta x_2 = [\Delta x_{2p}^2 + (b \cdot \theta \cdot 1/\cos^2\alpha)^2]^{1/2}$$

Pixel error

Mult. Scatt.



# Detector angular extension (position)



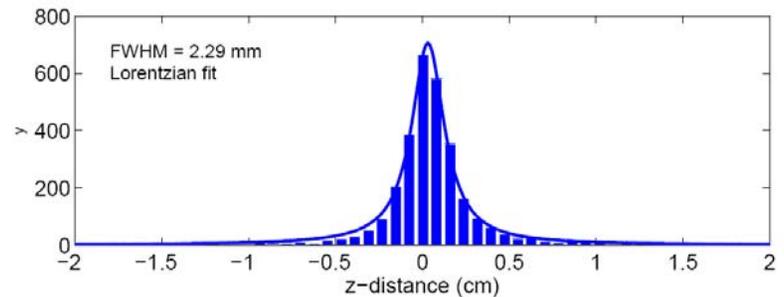
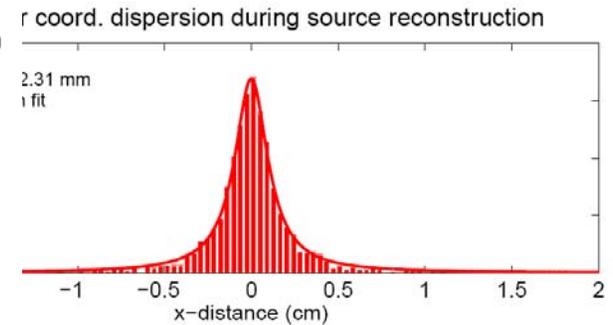
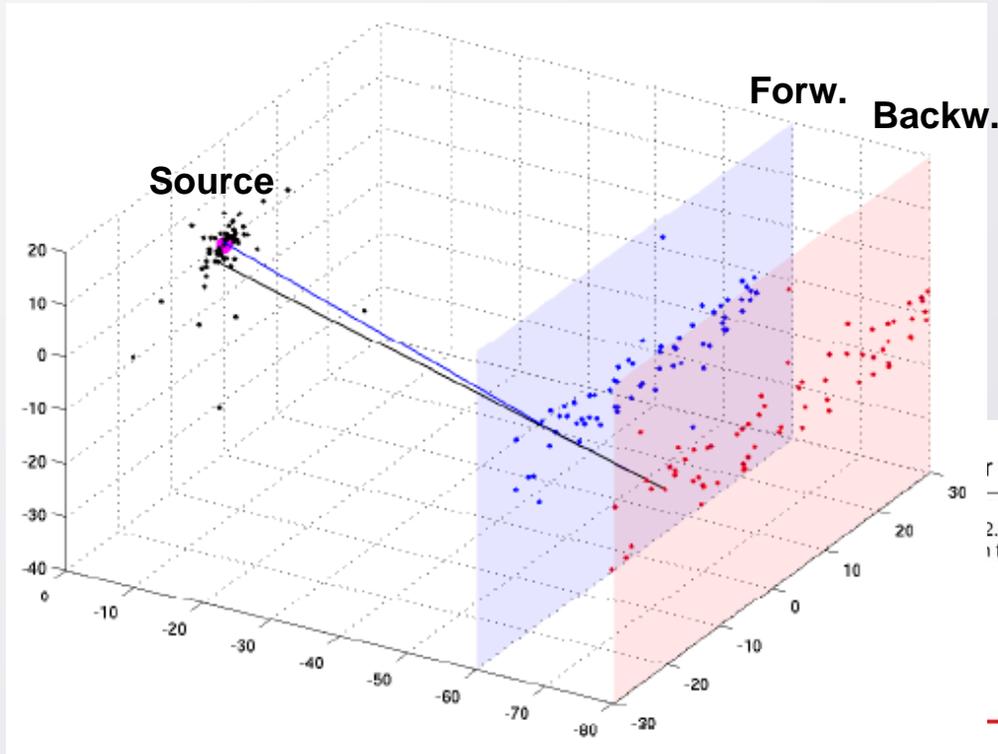
A very steep increase in error is expected for detectors at (or spanning) large angles:

$$\Delta x_3 = a \cdot \varphi/2 \cdot \mathbf{1/\cos^2\alpha}$$

$$1/\cos^2\alpha = \begin{cases} 1 & \text{for } \alpha = 0^\circ \\ 4/3 & \text{for } \alpha = 30^\circ \\ 2 & \text{for } \alpha = 45^\circ \end{cases}$$

**Conclusion:** Use a detector covering **30° or less**.

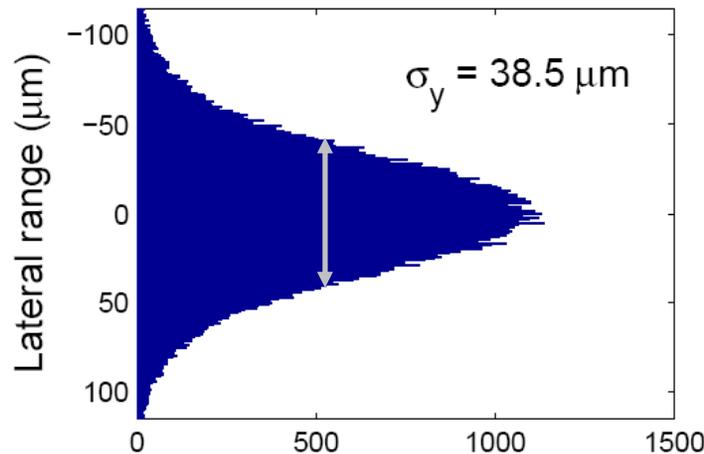
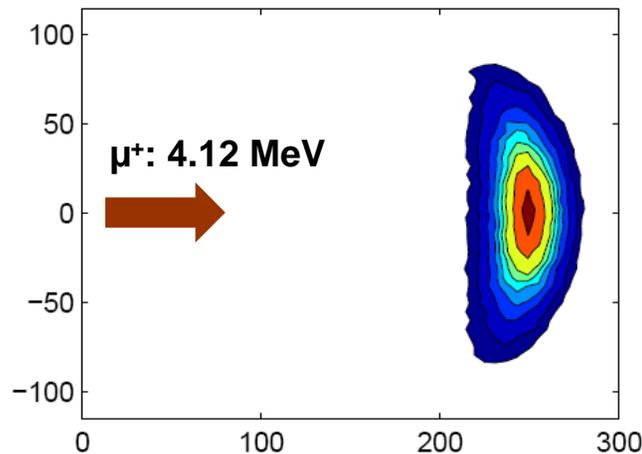
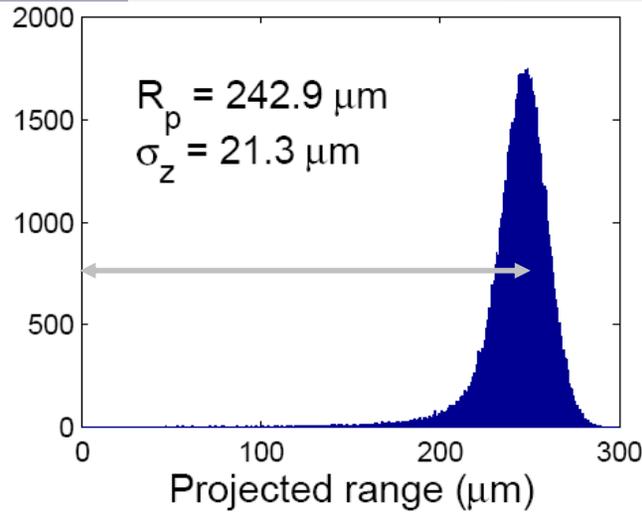
# Source position reconstruction





# Projected and lateral $\mu^+$ range in Ag

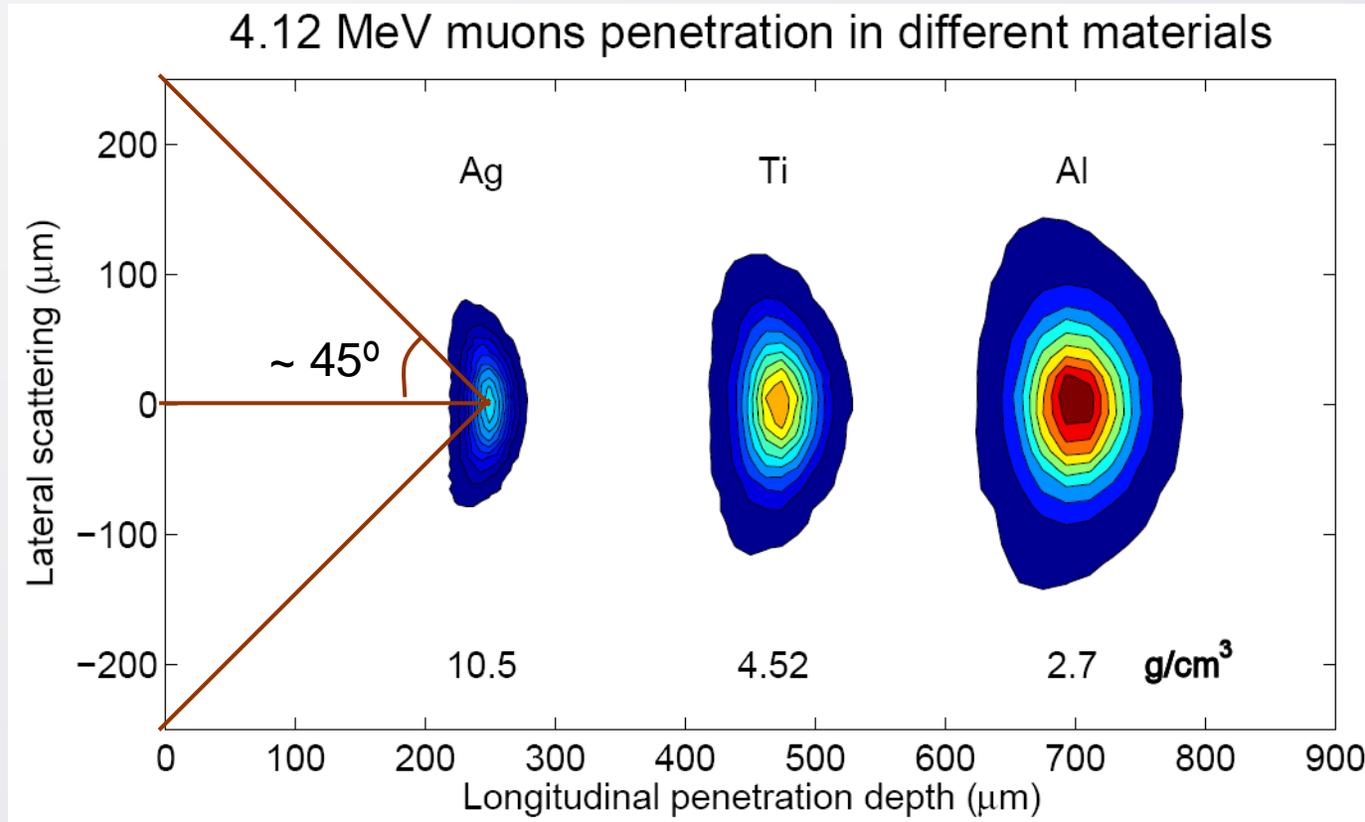
- The projected range relates to  $S_p$ , but how?
- Is lateral range important with respect to  $S_p$ ?
- Can we ignore the details in a quick GEANT4 simulation?



## Quick answer:

Yes, for Ag:  $13\sigma_y = S_p$   
Further studies for other elements.

# Projected and lateral $\mu^+$ ranges



Muon lateral range increases proportionately with projected range

Positrons are mainly (HWHM) emitted within  $\sim 45^\circ$  from muon beam direction